

# **Večskalne simulacije mehke in biološke snovi**

Matej Praprotnik

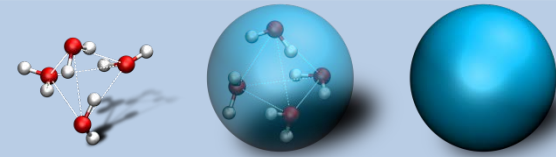
Računske in statistične metode v kemiji

Kemijski inštitut, 19.-21. oktober 2021



NATIONAL INSTITUTE OF CHEMISTRY

# Outline



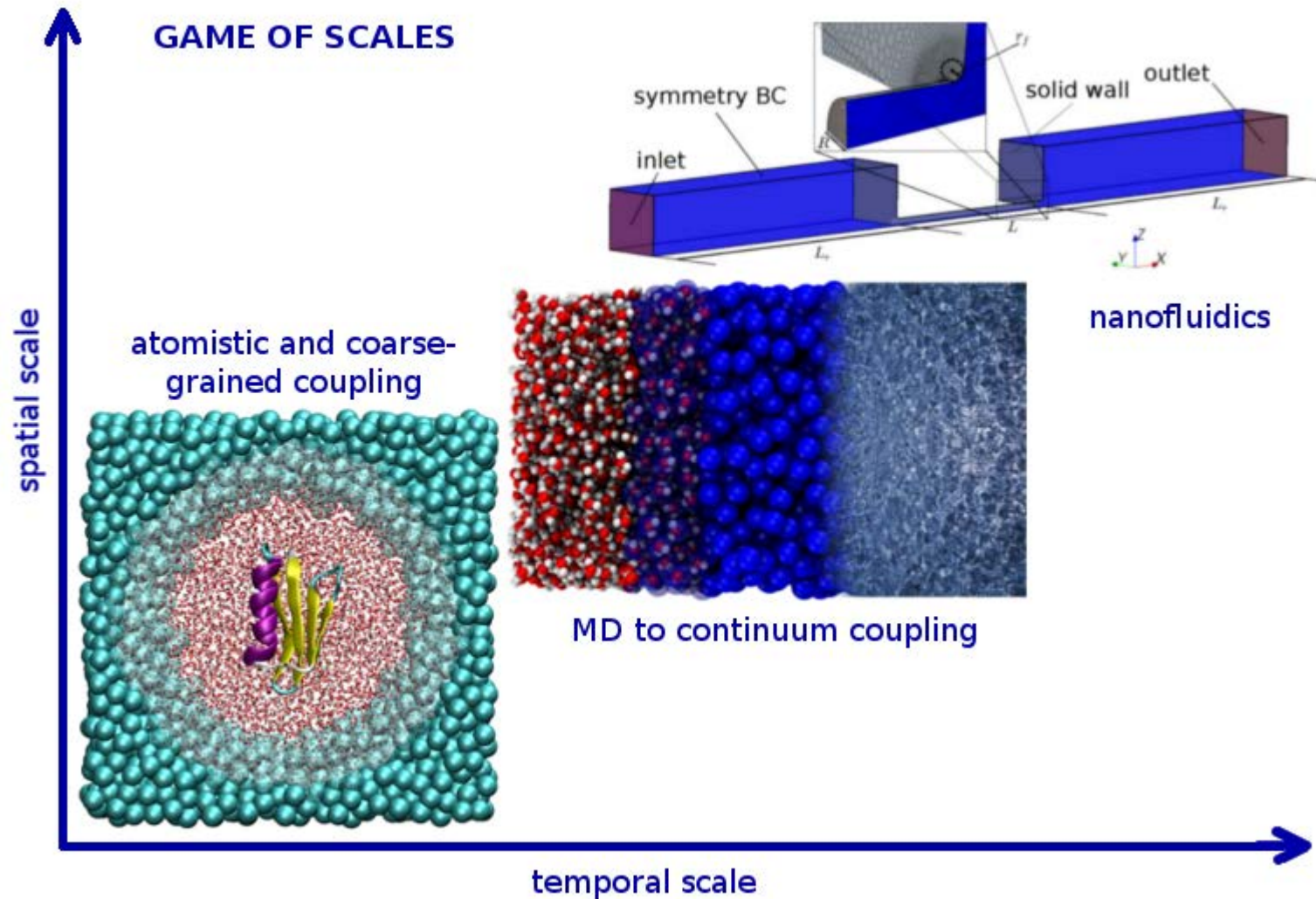
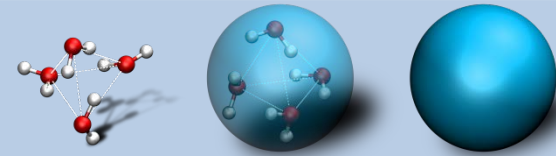
## ➤ multiscale simulations:

1. Adaptive Resolution Scheme (AdResS)
2. coupling to supramolecular coarse-grained models
3. Open Boundary Molecular Dynamics (OBMD)

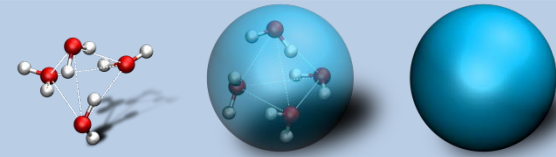
## ➤ biomolecular applications:

1. DNA molecule in salt solution
2. columnar phases of DNA
3. OBMD of a DNA molecule

# Multiscale modeling & simulation



# Multiscale simulation



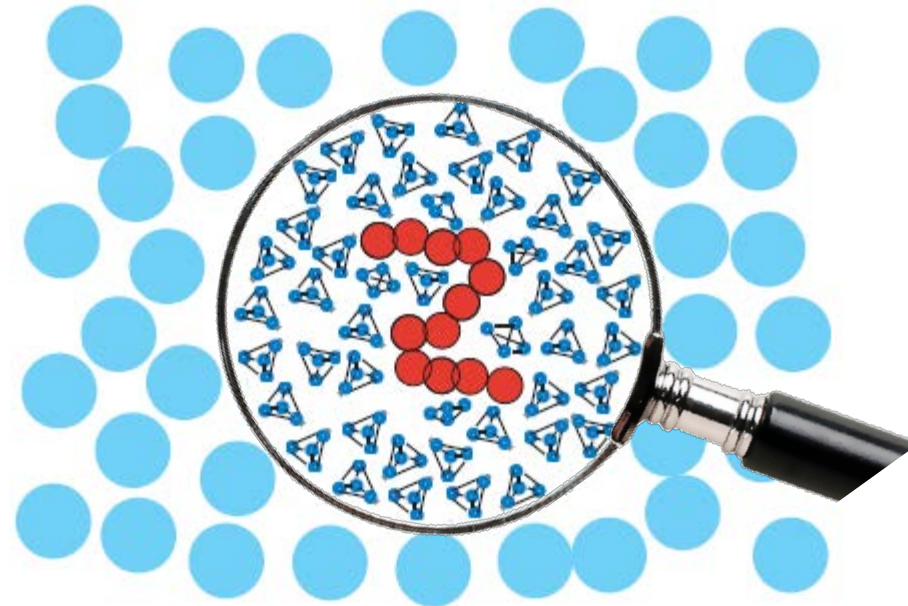
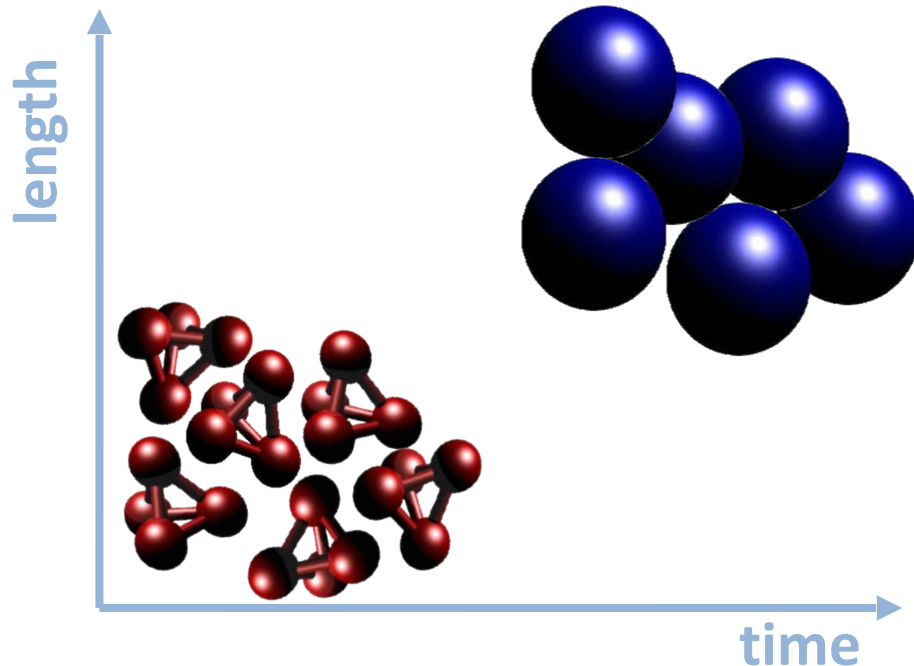
## ➤ atomistic simulation

- large length and time scales are difficult to capture

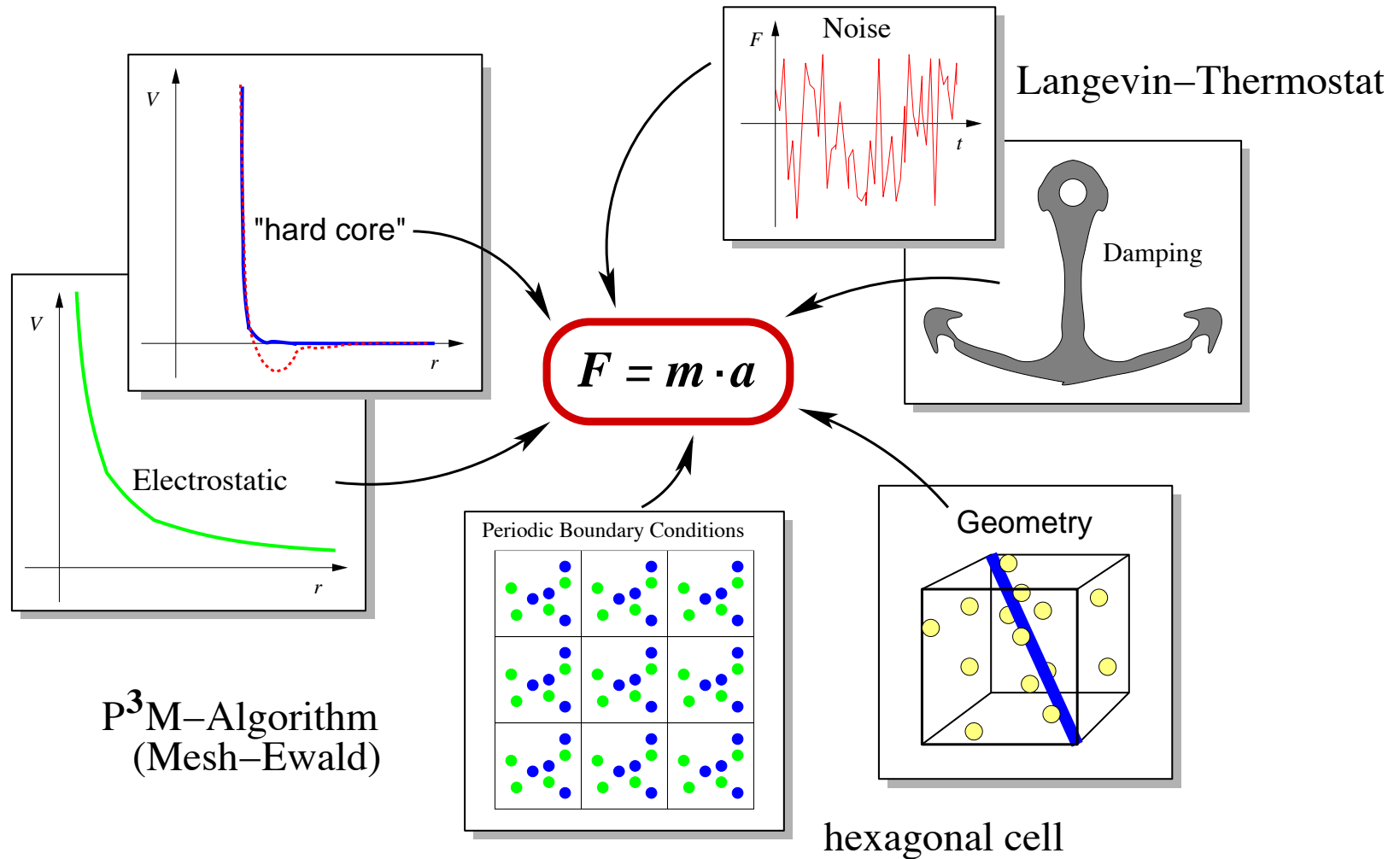
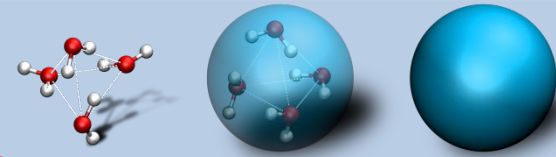
## ➤ coarse-grain simulation

- atomistic details are lost

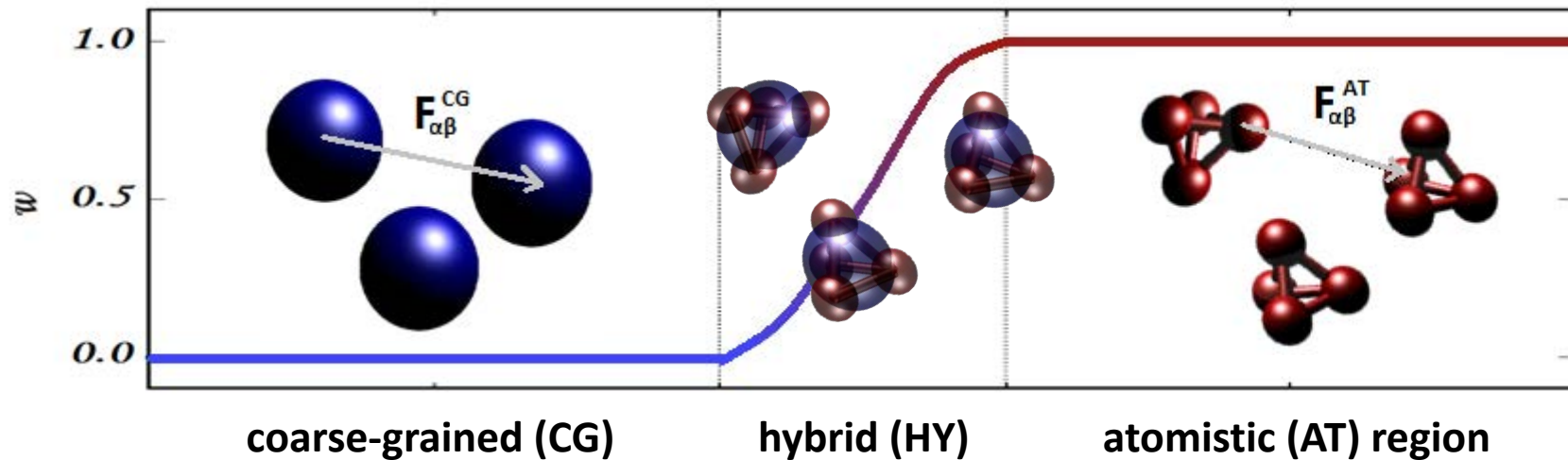
## ➤ multiscale simulation



# Molecular Dynamics



# Adaptive Resolution Scheme (AdResS)



➤ force between particle  $\alpha$  and  $\beta$ :

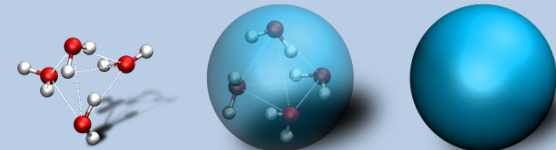
$$F_{\alpha}^{AdResS} = \sum_{\beta \neq \alpha} w(|R_{\alpha} - R|) w(|R_{\beta} - R|) F_{\alpha\beta}^{AT} + \sum_{\beta \neq \alpha} \left[ 1 - w(|R_{\alpha} - R|) w(|R_{\beta} - R|) \right] F_{\alpha\beta}^{CG} - F_{\alpha}^{TD}(|R_{\alpha} - R|)$$

$w(r)$ ... position dependent weighting function

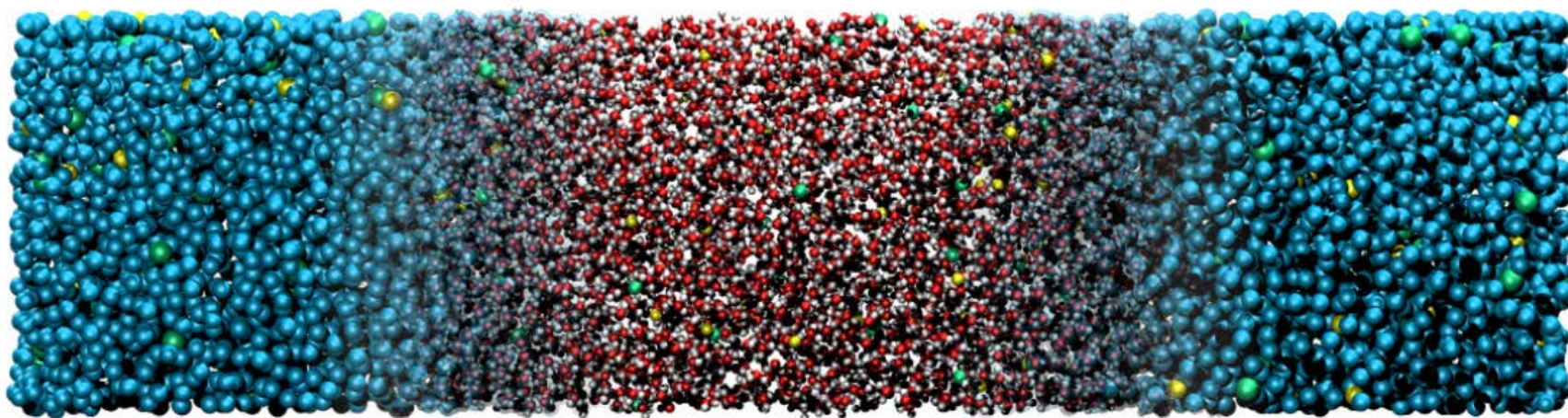
➤ above force coupling scheme obeys Newton's third law



# Multiscale 1M NaCl salt solution



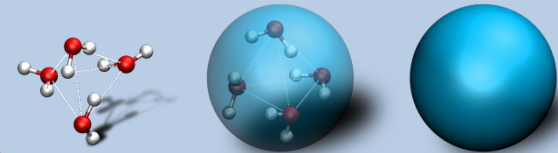
- atomistic force field:  
TIP3P + Amber 03
- coarse-grained force field:  
derived with Boltzmann inversion



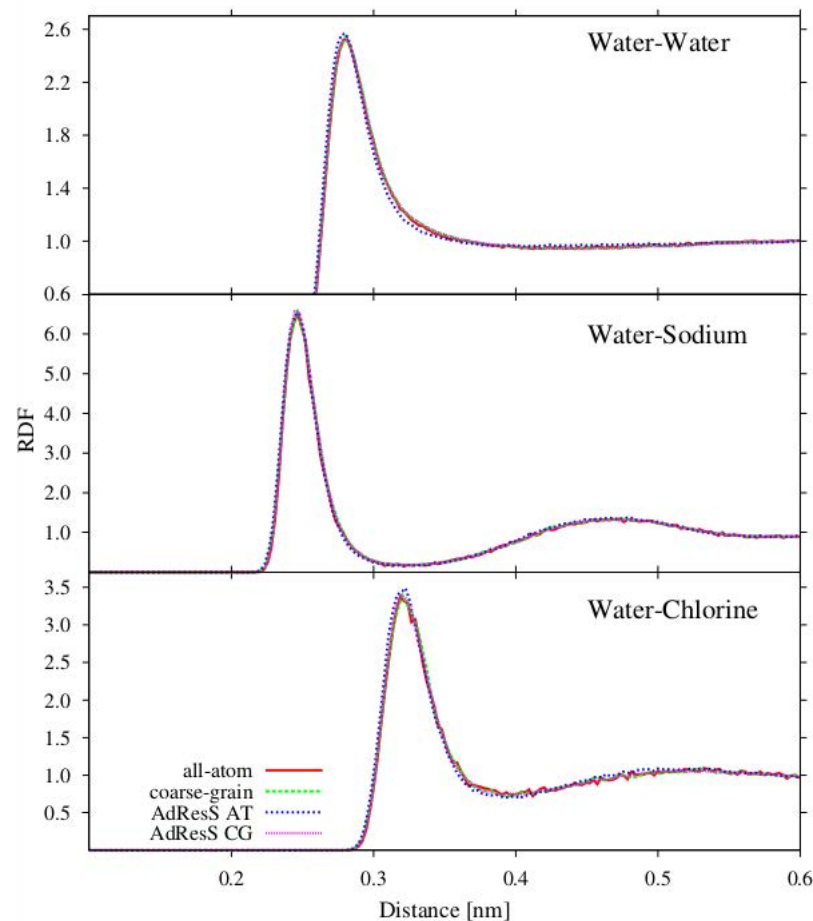
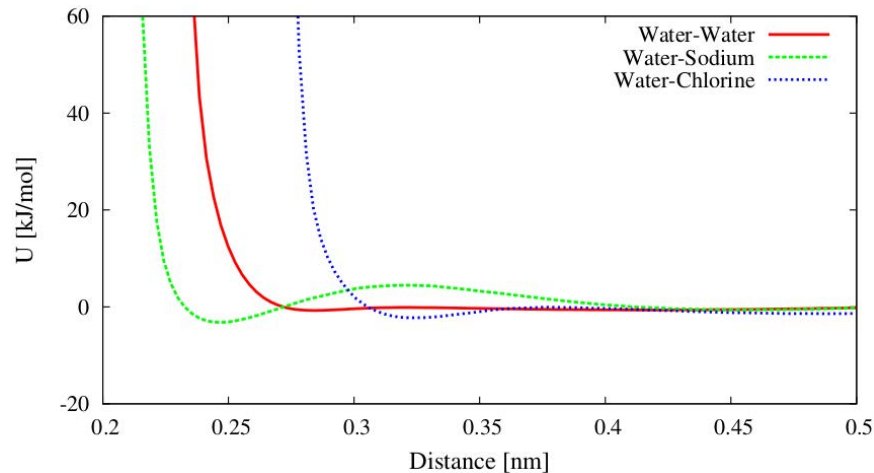
Bevc, Junghans, Kremer, Praprotnik; *New. J. Phys.* (2013)

Zavadlav, Podgornik, Praprotnik; *JCTC* (2015)

# Multiscale 1M NaCl salt solution

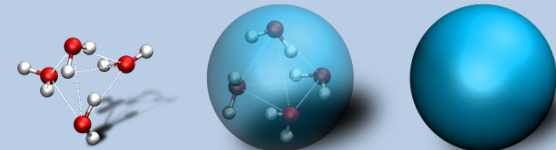


➤ derived CG potential



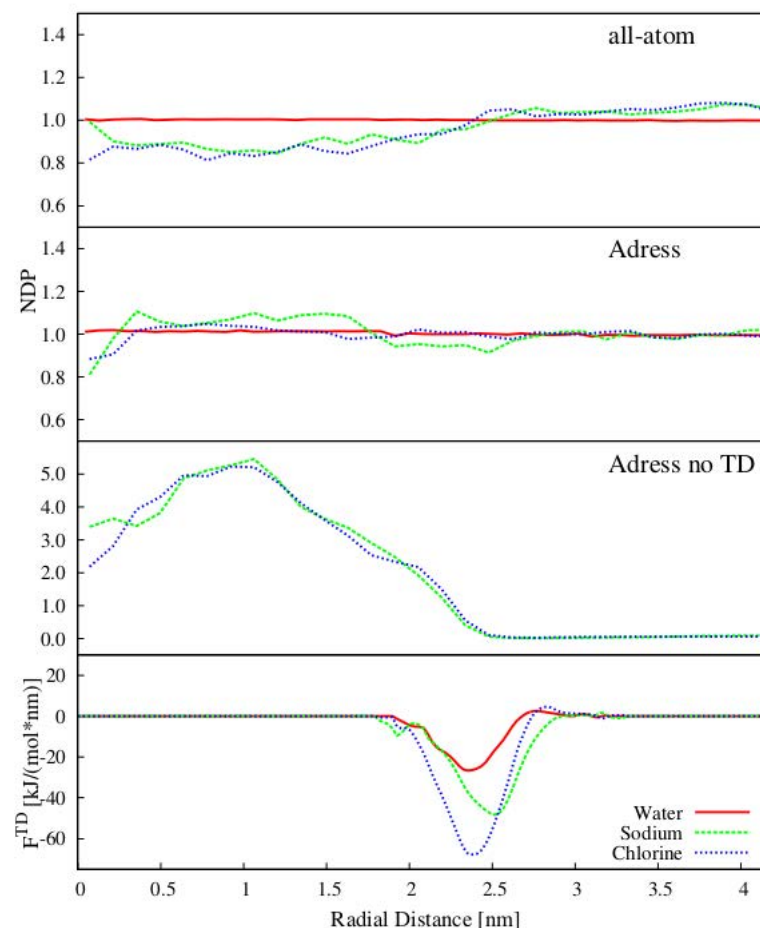


# Multiscale 1M NaCl salt solution

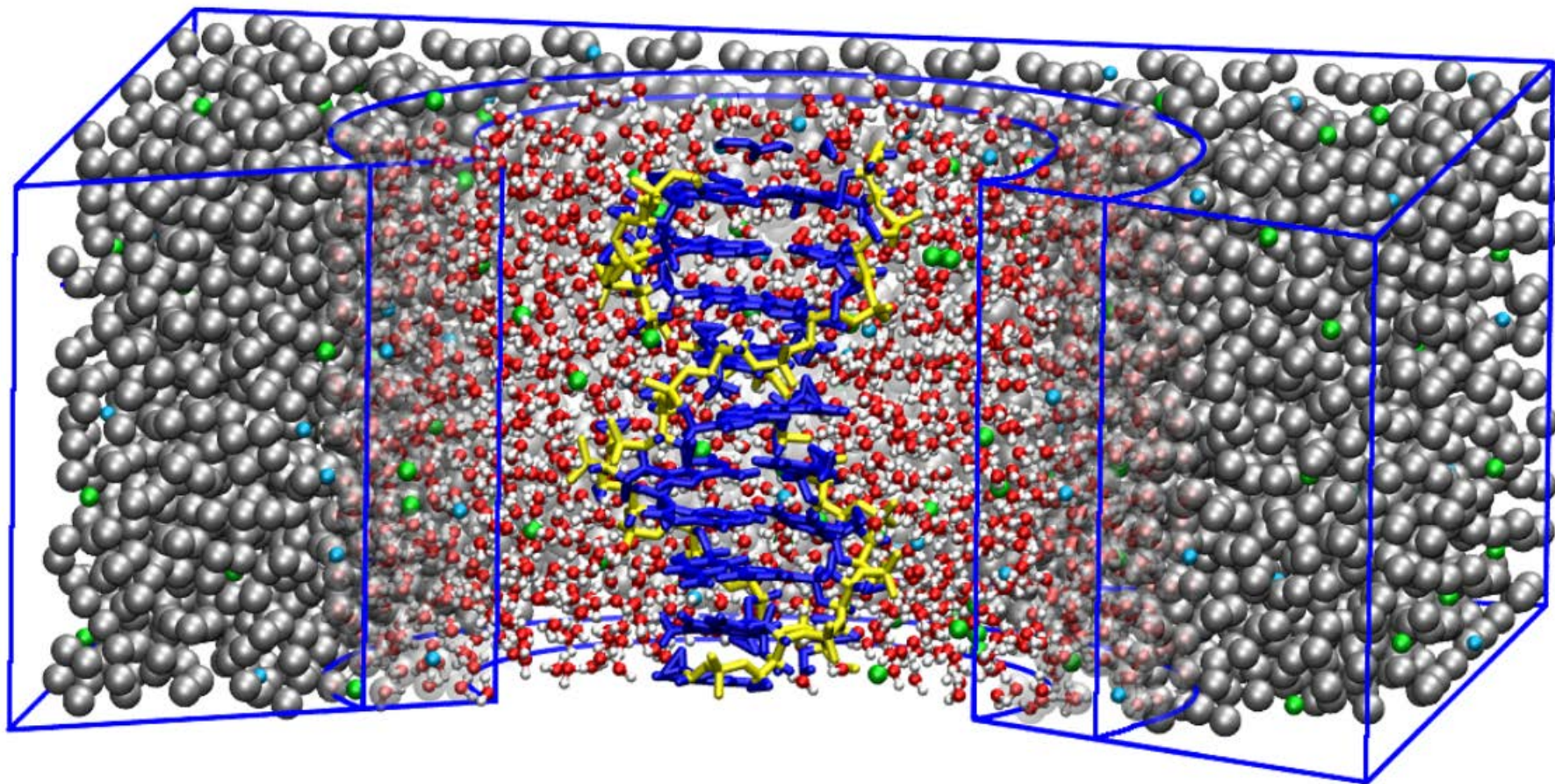
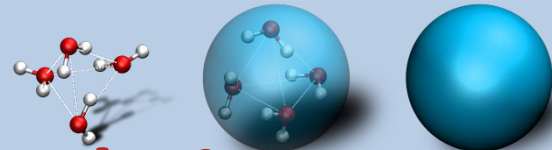


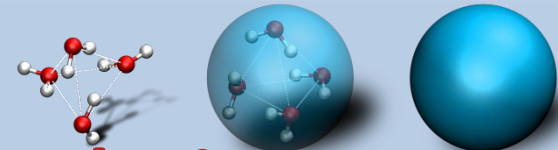
- density profile
- thermodynamic (TD) force on CG beads in HY region
- calculated iteratively

$$F_{TD}^{i+1} = F_{TD}^i - \frac{M_\alpha}{\rho_0^2 \kappa_T} \nabla \rho^i(x)$$



# Atomistic DNA in multiscale salt solution

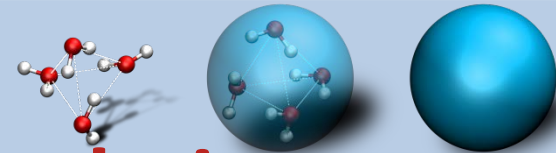




# DNA molecule in multiscale salt solution

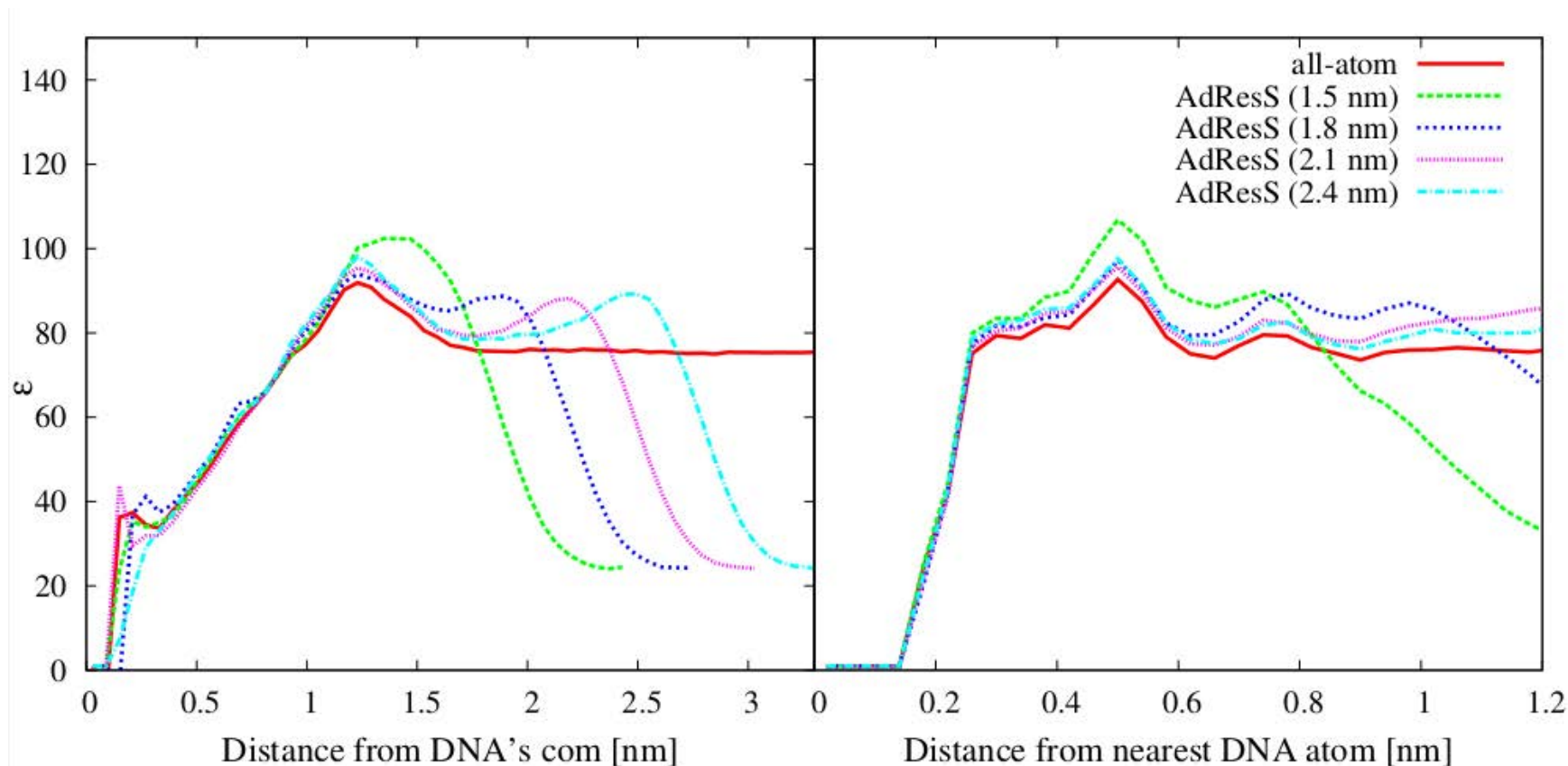
➤ dielectric constant of DNA molecule

Group	$\epsilon$ (1.5 nm)	$\epsilon$ (1.8 nm)	$\epsilon$ (2.1 nm)	$\epsilon$ (2.4 nm)	$\epsilon$ ( $\infty$ )
Phosphate	18.3	21.1	17.3	15.7	17.0
Sugar	2.7	2.8	2.7	2.4	2.6
Base	2.1	2.1	2.0	2.0	2.1
DNA	5.6	5.9	5.4	4.5	5.0

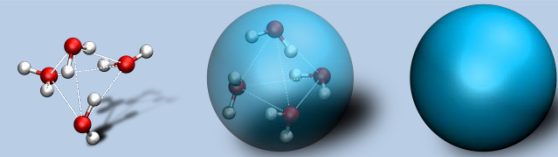


# DNA molecule in multiscale salt solution

➤ dielectric constant of water



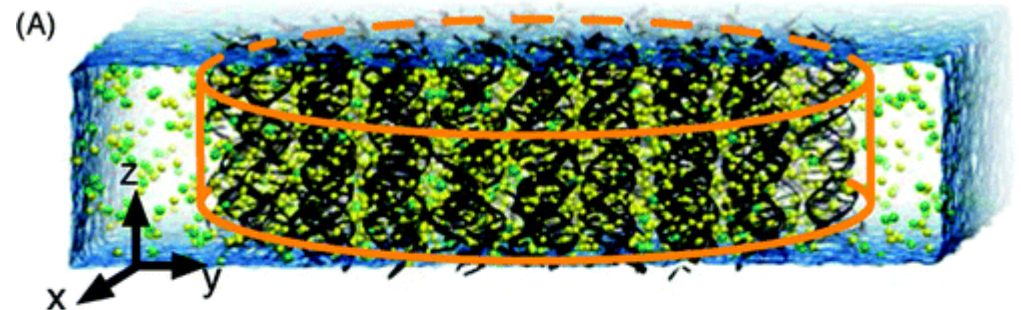
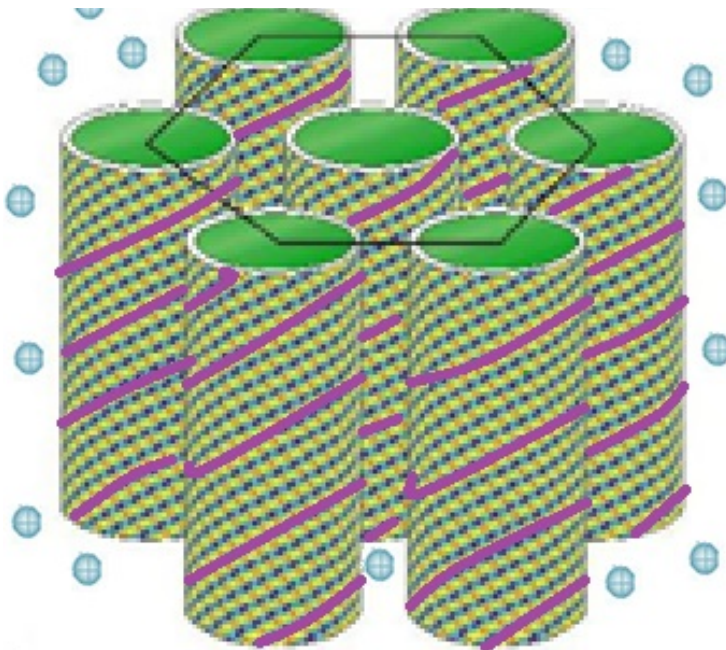




# Columnar phases of DNA arrays

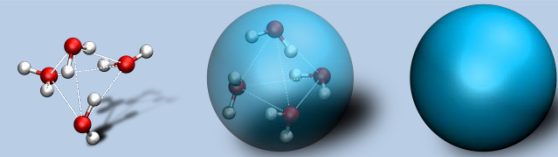
Isotropic	Cholesteric	Hexagonal 2D progressive longitudinal ordering	Orthorhombic
$C(\text{mg/ml}) \approx$	160 (*)	380	670
	mean interhelices distance $a_m$	intermolecular distance $a_H$	lattice parameters
	49 Å    32 Å	31.5 Å    29 Å    23.7 Å	$a = 24.09 \text{ Å}$ $a = 20.77 \text{ Å}$ $b = 39.33 \text{ Å}$ $b = 29.72 \text{ Å}$
		helix pitch P	
		34.6 Å ..... 30.2 Å	

Durand, Doucet, Livolant, *J. Phys. II France* (1992)



Lyubartsev, Nordenskiöld, *J. Phys. Chem.* (1995), Yoo, Aksimentiev, *J. Phys. Chem. Lett.* (2011)





# Columnar phases of DNA arrays

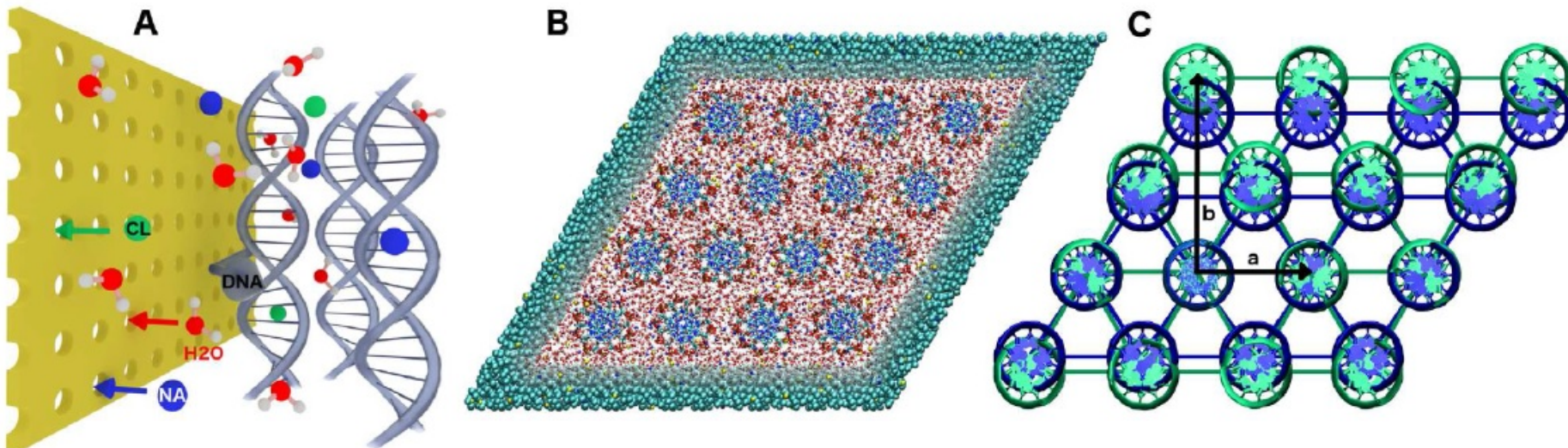
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		helix pitch P	
		34.6 Å	30.2 Å

➤ system of 16 DNA molecules

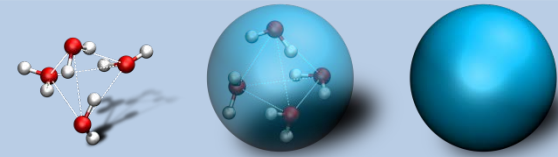
➤ hexagonal/orthorhombic

➤  $\text{Na}^+/\text{Spd}^{3+}$

Durand, Doucet, Livolant, *J. Phys. II France* (1992)

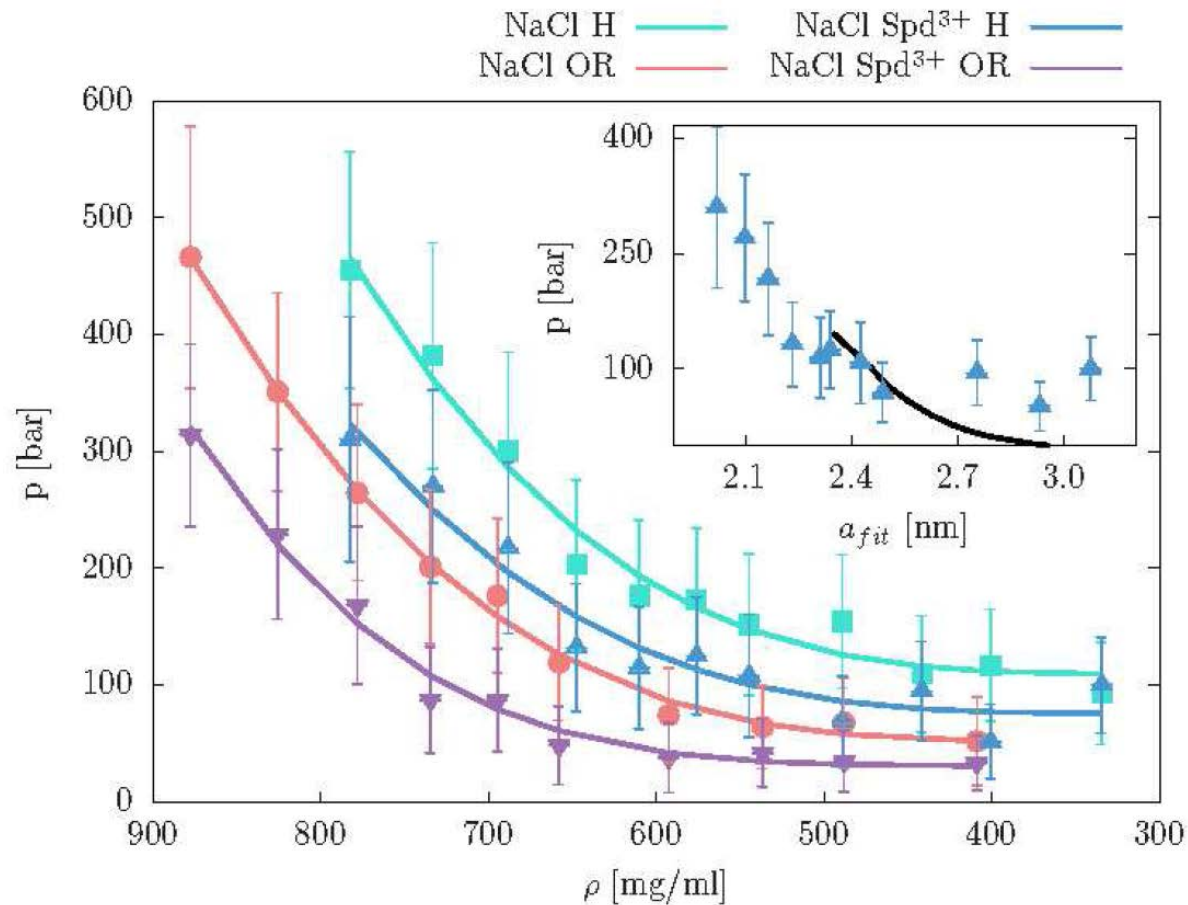


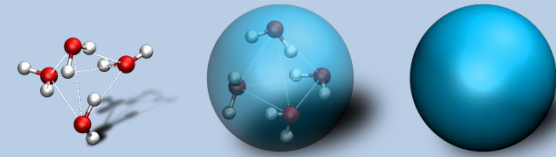
Zavadlav, Podgornik, Praprotnik; *Sci. Rep.* (2017)



# Columnar phases of DNA arrays

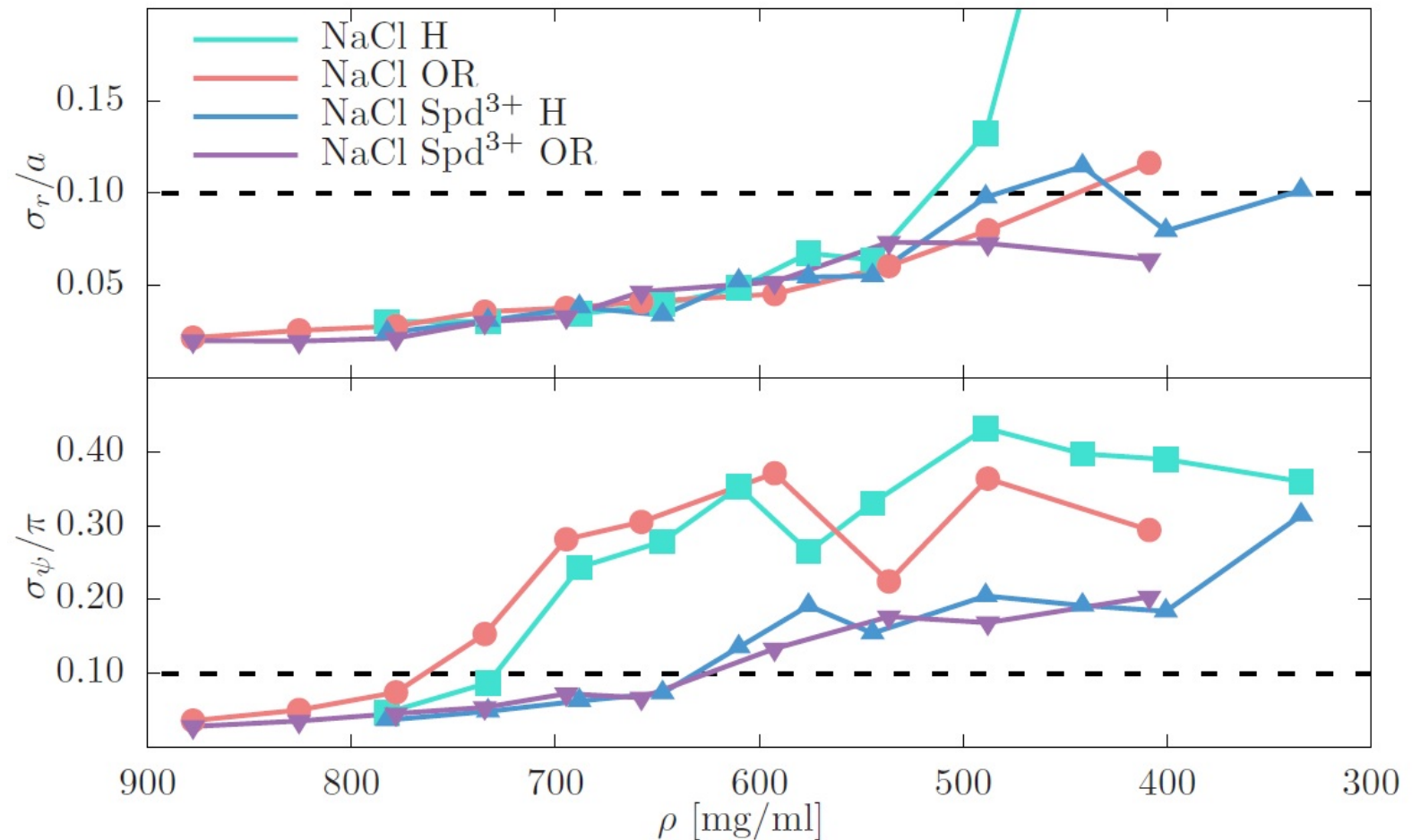
➤ osmotic pressure vs. DNA density



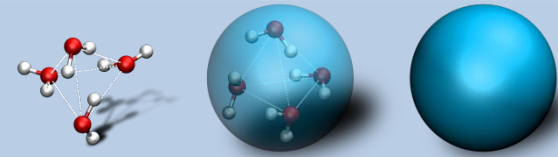


# Columnar phases of DNA arrays

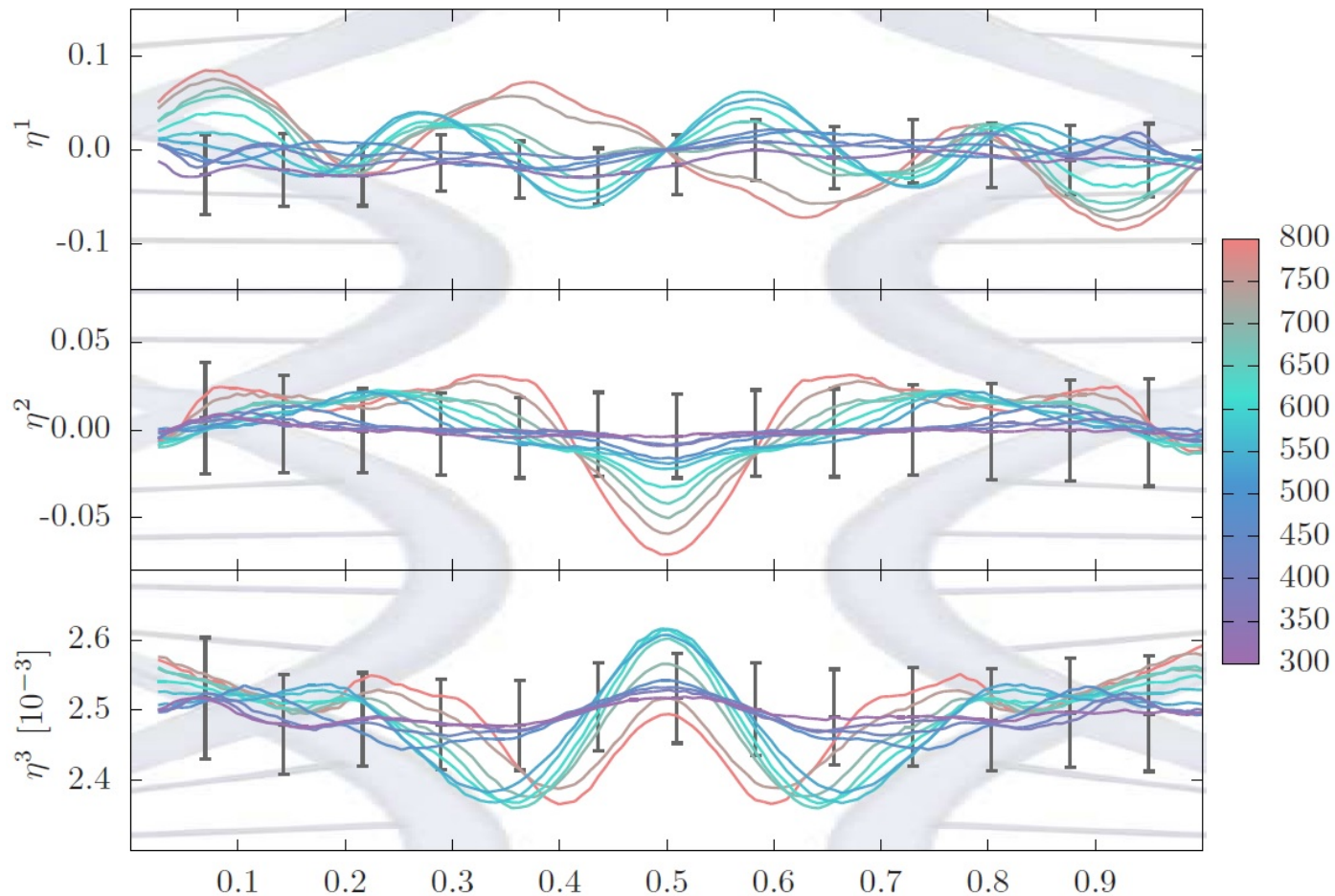
➤ positional and orientational correlations



# Columnar phases of DNA arrays



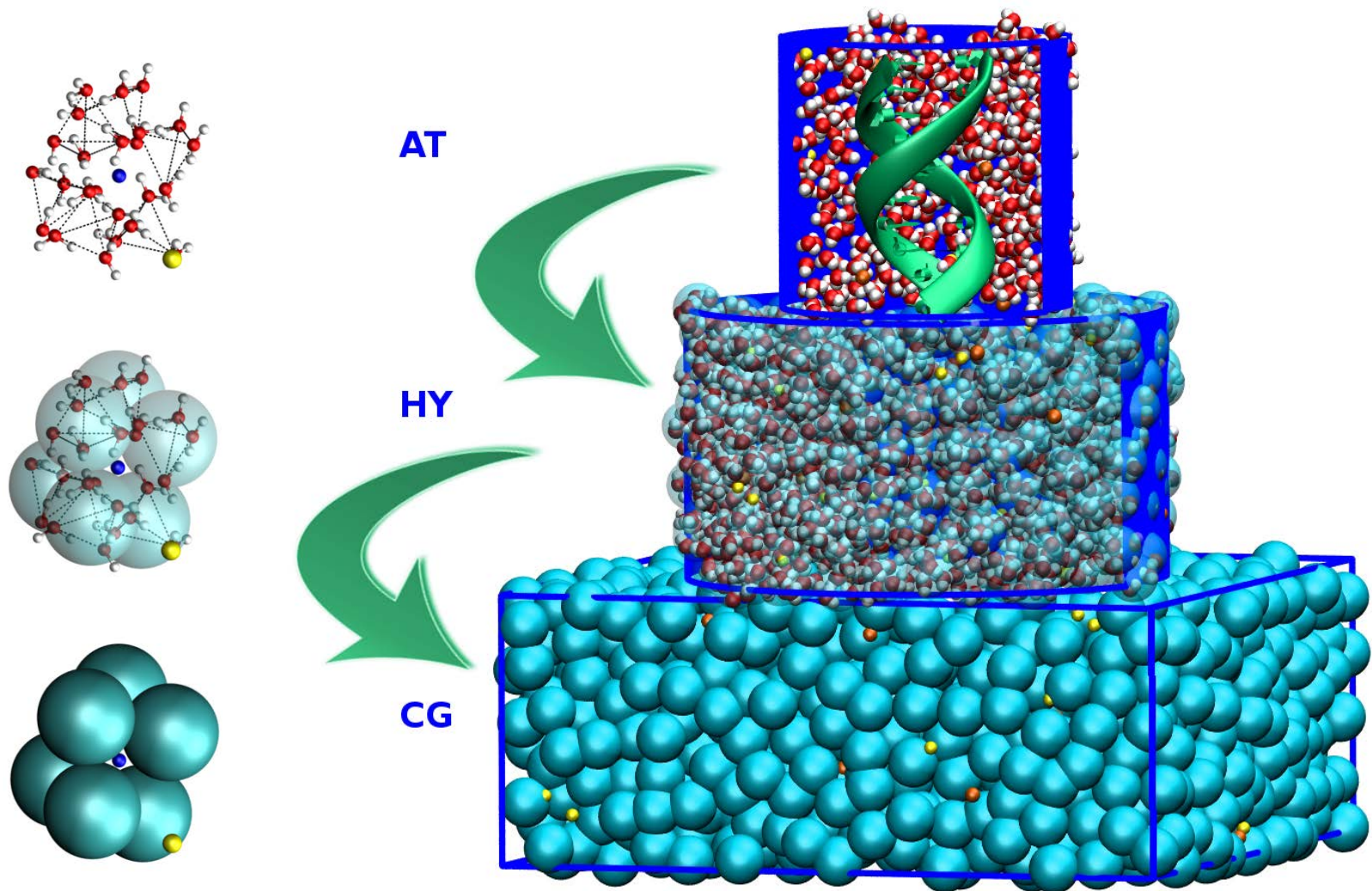
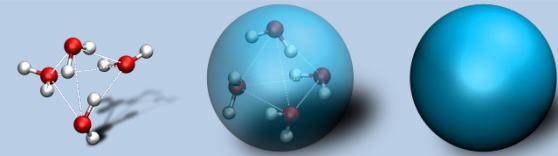
➤ order parameters



Zavadlav, Podgornik, Praprotnik; *Sci. Rep.* (2017)

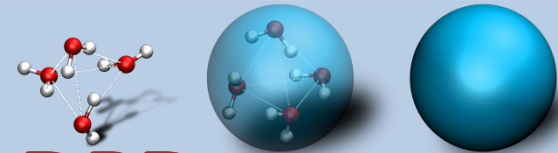


# DNA molecule in bundled-SPC/MARTINI salt solution



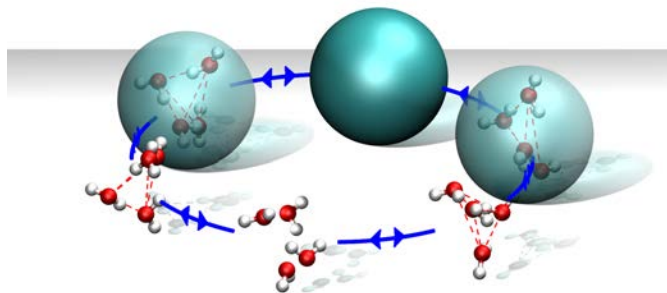


# Free SPC/MARTINI water and DPD



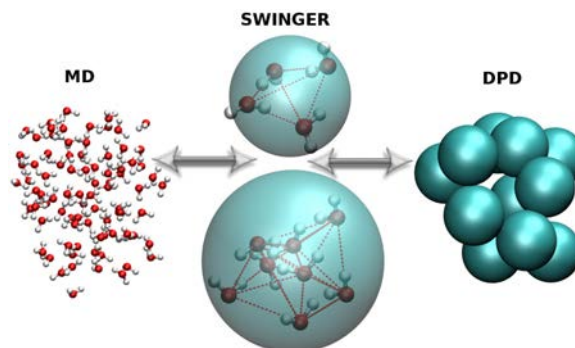
## ➤ Algorithm SWINGER:

- concurrently assembles, disassembles and reassembles water clusters



## ➤ DPD:

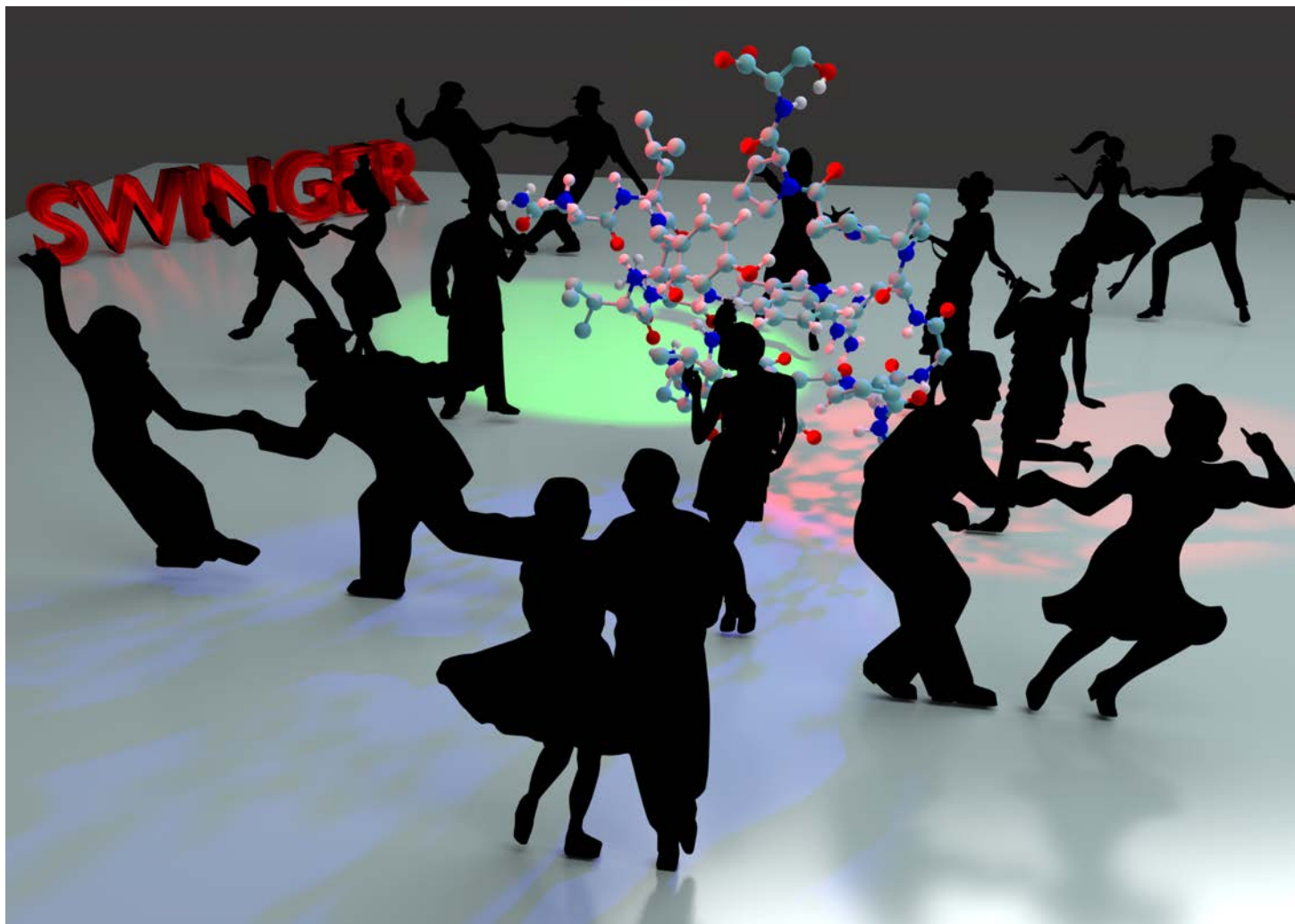
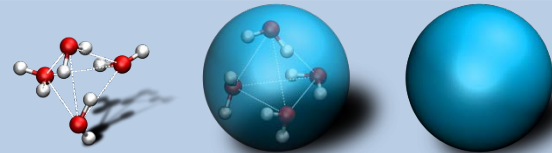
- supramolecular coupling of atomistic water with DPD



Zavadlav, Marrink, Praprotnik; *J. Chem. Theory Comput.* (2016)

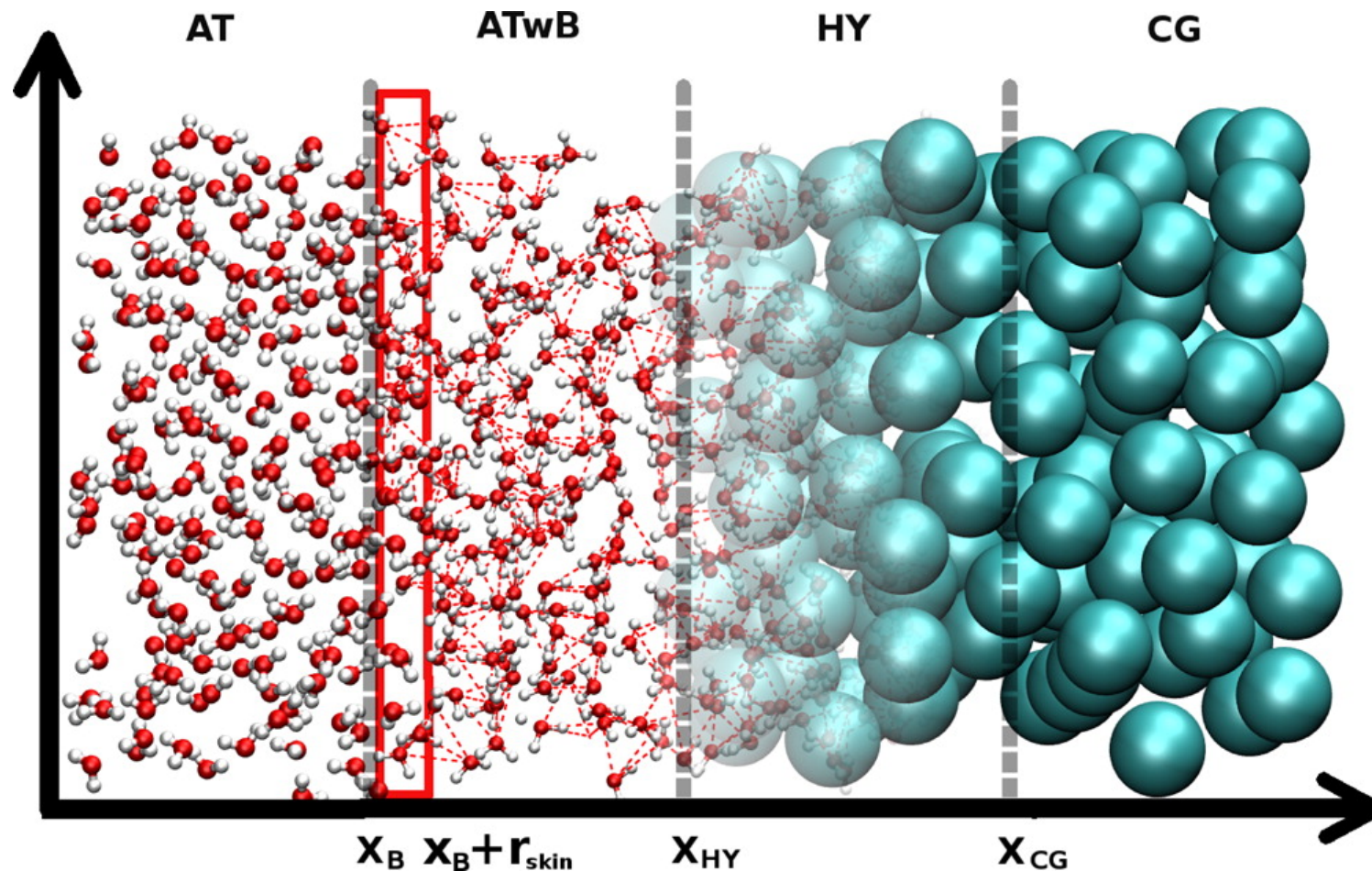
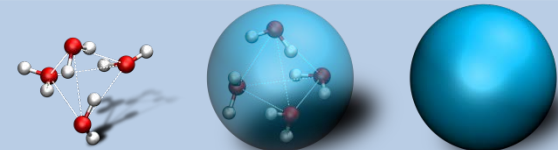
Zavadlav, Praprotnik; *J. Chem. Phys.* (2017)

# SWINGER algorithm

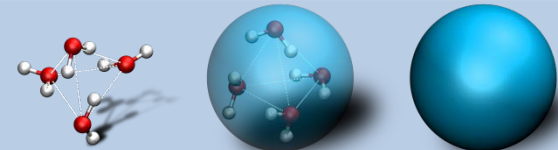


Zavadlav, Marrink, Praprotnik; *JCTC* (2018)

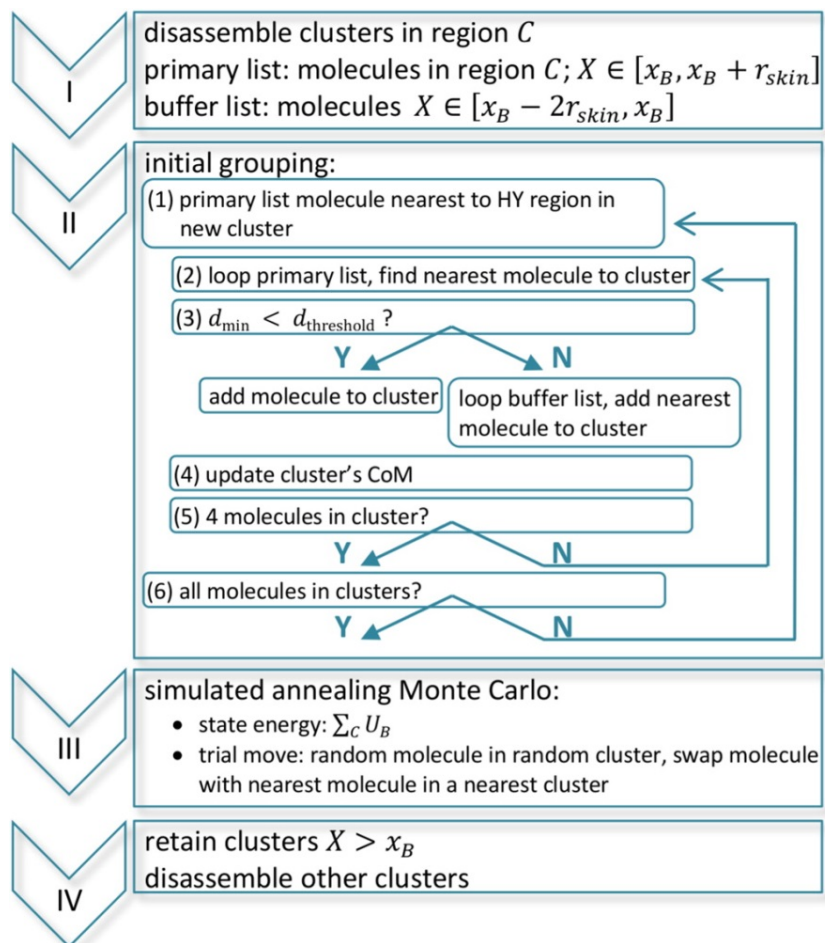
# Free SPC/MARTINI water



# Free SPC/MARTINI water

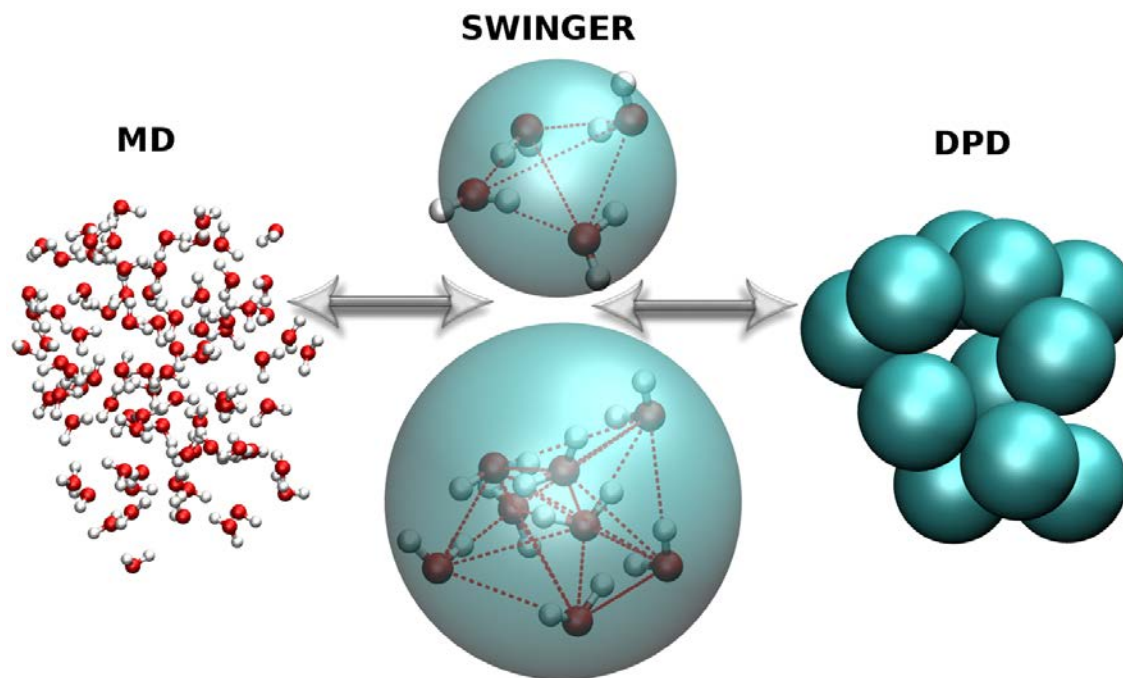
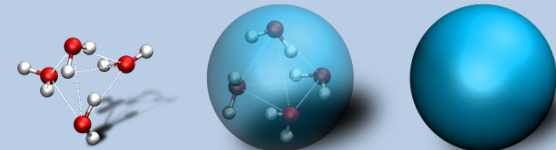


## ➤ SWINGER algorithm





# MD/DPD water



MD:

$$\mathbf{F}_{ij}^{MD,C}(\mathbf{r}_{ij}) = -\frac{\partial U^{MD}}{\partial \mathbf{r}_{ij}}$$

DPD:

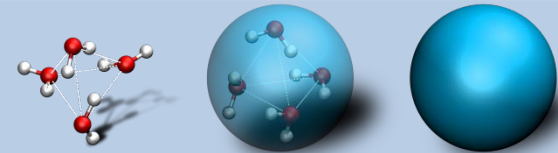
$$\mathbf{F}_{\alpha\beta}^{DPD,C}(\mathbf{R}_{\alpha\beta}) = a_{\alpha\beta}(1 - R_{\alpha\beta}/R_c)\hat{\mathbf{R}}_{\alpha\beta}$$

$$\mathbf{F}_{\alpha\beta}^{DPD,R}(\mathbf{R}_{\alpha\beta}) = \sqrt{2\gamma_{\alpha\beta}k_B T}(1 - R_{\alpha\beta}/R_c)\zeta_{ij}\hat{\mathbf{R}}_{\alpha\beta}$$

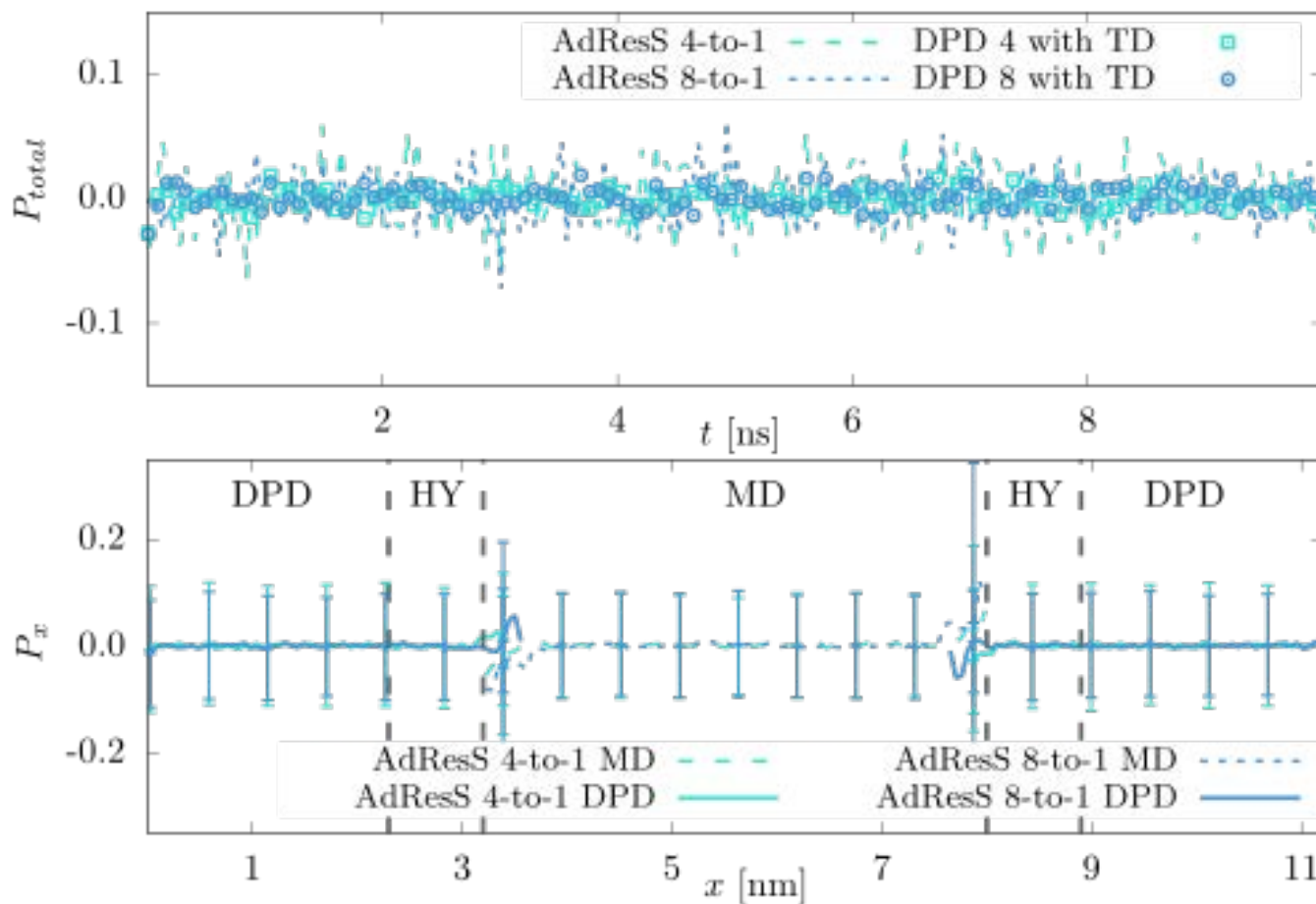
$$\mathbf{F}_{\alpha\beta}^{DPD,D}(\mathbf{R}_{\alpha\beta}) = -\gamma_{\alpha\beta}(1 - R_{\alpha\beta}/R_c)^2(\hat{\mathbf{R}}_{\alpha\beta} \cdot \mathbf{V}_{\alpha\beta})\hat{\mathbf{R}}_{\alpha\beta}$$



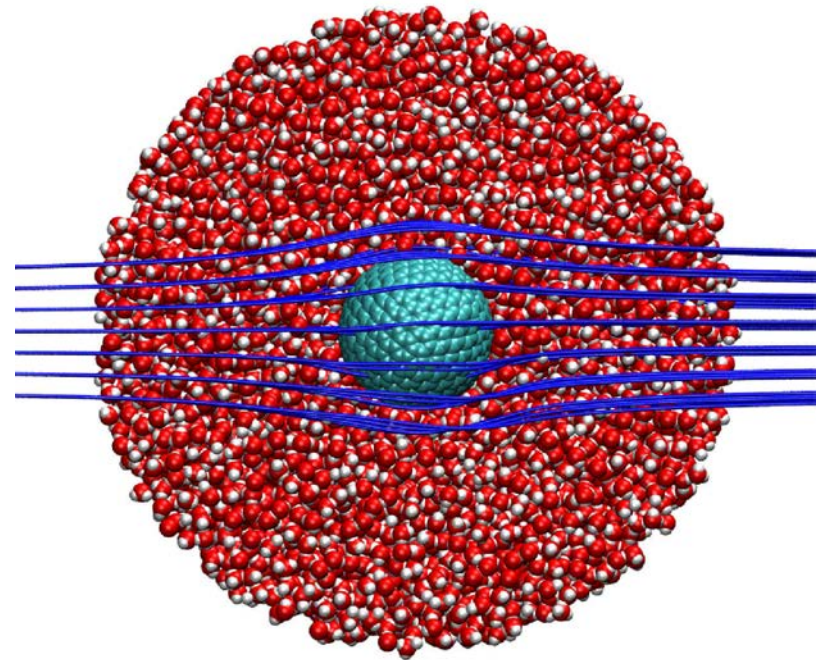
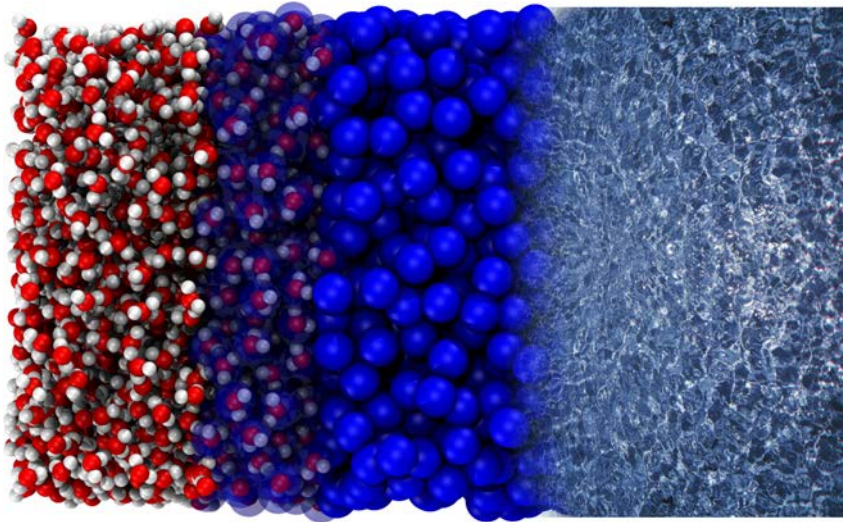
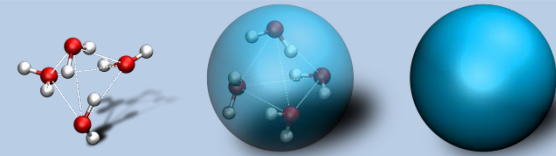
# MD/DPD water



➤ conservation of linear momentum

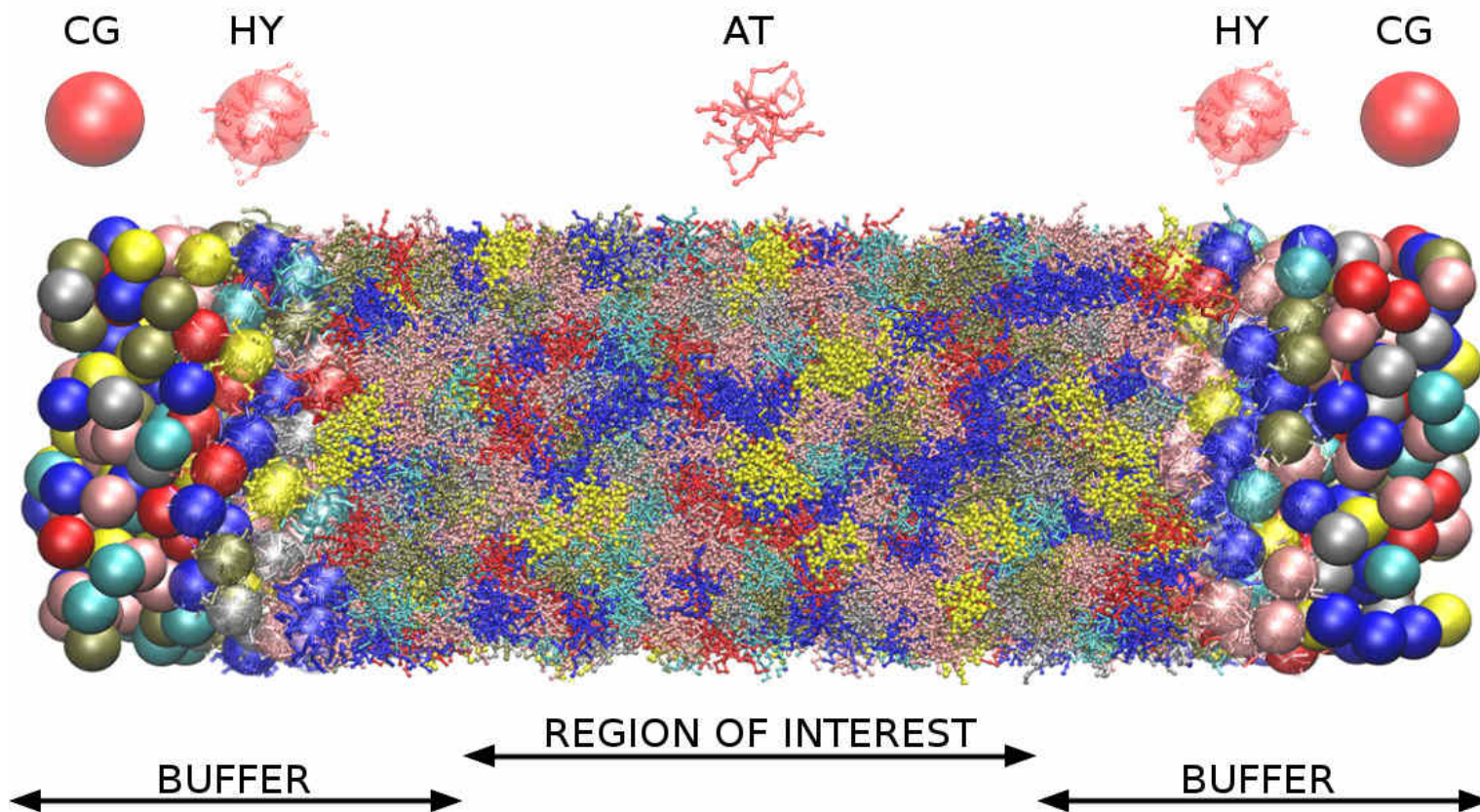
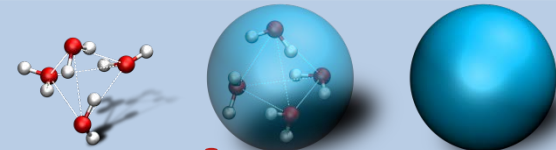


# Coupling to CFD



Delgado-Buscalioni, Sablić, Praprotnik; *Eur. Phys. J. Special Topics* (2015)  
Walther et al.; *J. Comput. Phys.* (2012)

# Open Boundary Molecular Dynamics



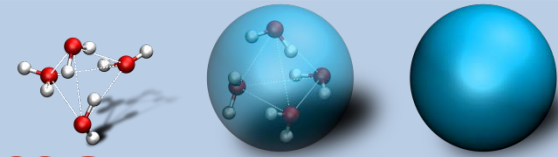
Delgado-Buscalioni, Sablić, Praprotnik; *Eur. Phys. J. Special Topics* (2015)

Sablić, Praprotnik, Delgado-Buscalioni; *Soft Matter* (2016)

Delle Site, Praprotnik; *Phys. Rep.* (2017)



# Thermodynamic systems



## ➤ isolated systems:

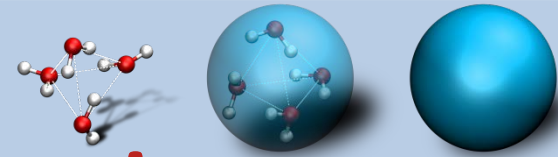
1. no exchange of matter and energy with the surroundings

## ➤ closed systems:

1. exchange of energy, no exchange of matter
2. constant number of particles

## ➤ open systems:

1. exchange of matter and energy
2. number of particles fluctuates



# Open Boundary Molecular Dynamics

➤ system exchanges mass, momentum, and energy with its surroundings

1. Insertion of molecules:  $\Delta N_B = \frac{\Delta t}{\tau_r} \left( \alpha \langle N_B \rangle - N_B \right)$
2. Multiscale buffers -> facilitates insertion

➤ external boundary condition

1. Linear momentum conservation

2. Additional force in buffers:  $F^{ext} = J \cdot n_B A + \frac{P_{out} - P_{in}}{\Delta t} + \sum F_{\alpha}^{TD}$

➤ DPD thermostat:  $F_{\alpha}^{thermo} = \sum_{i \in \alpha, j \in \beta, \alpha \neq \beta} \sigma \omega^R(r_{ij}) \zeta_{ij} \hat{r}_{ij} - \gamma \omega^D(r_{ij}) (\hat{r}_{ij} \cdot v_{ij}) \hat{r}_{ij}$

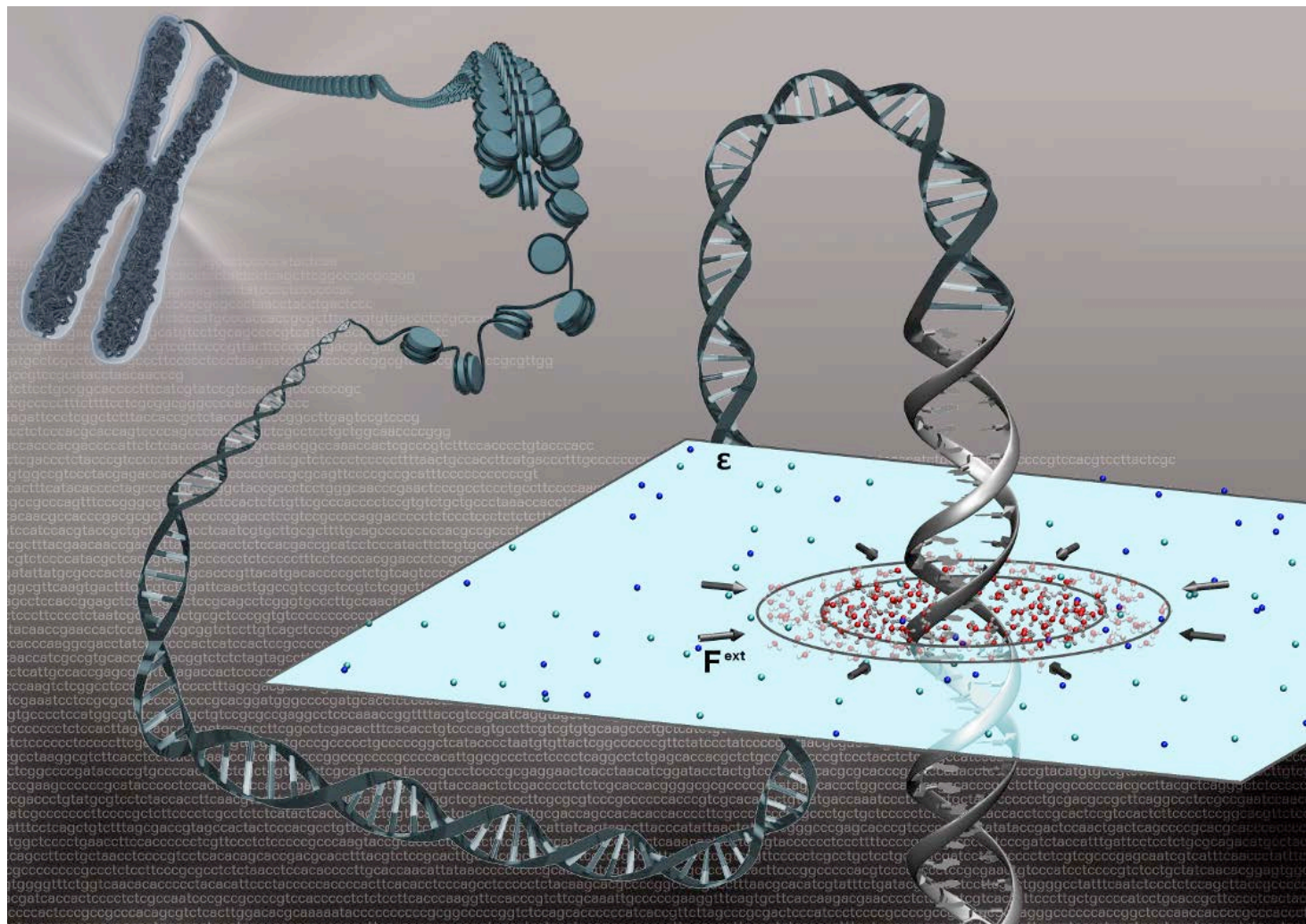
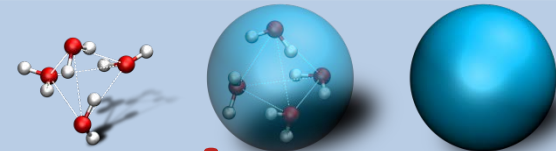
➤ total force on each particle:

$$\omega^D(r_{ij}) = \left[ \omega^R(r_{ij}) \right]^2 \sigma^2 = 2k_B T \gamma$$

$$F_{\alpha} = F_{\alpha}^{AdResS} + F_{\alpha}^{ext} + F_{\alpha}^{thermo}$$

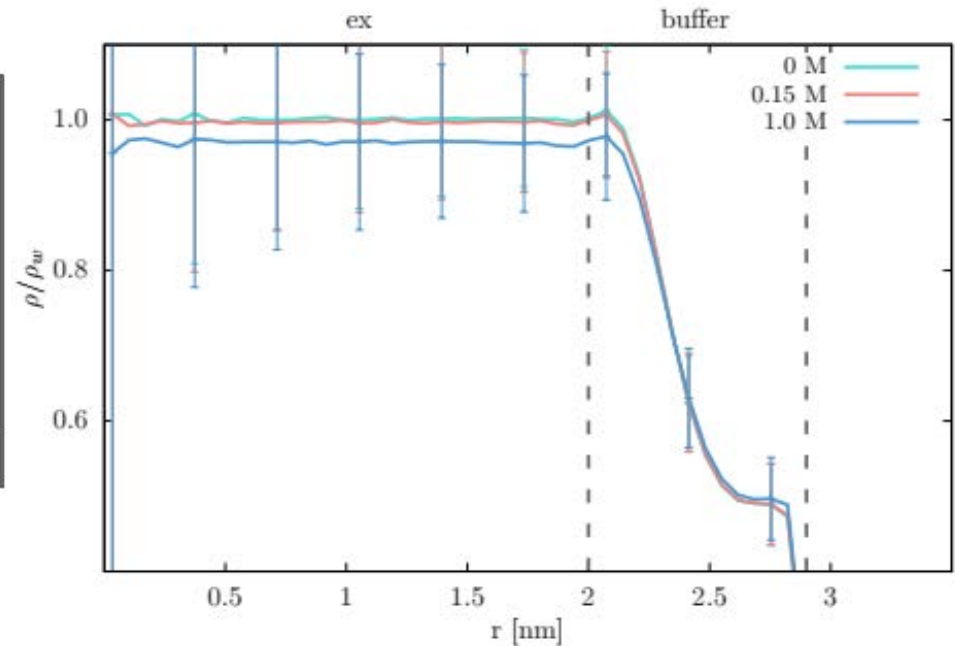
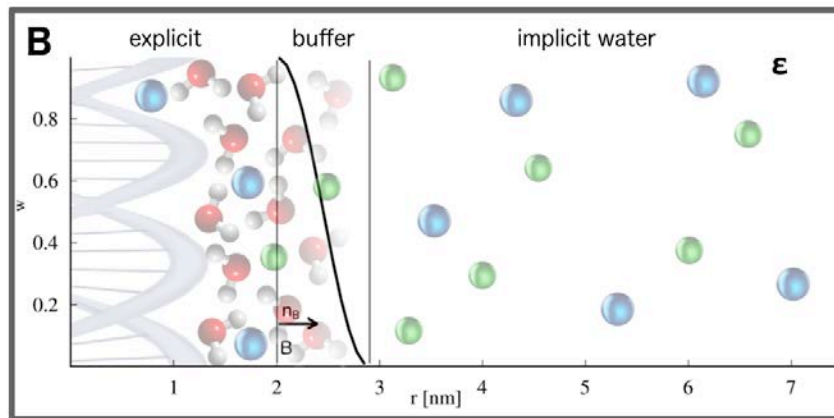
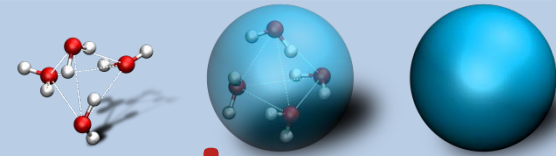


# Open Boundary Molecular Dynamics

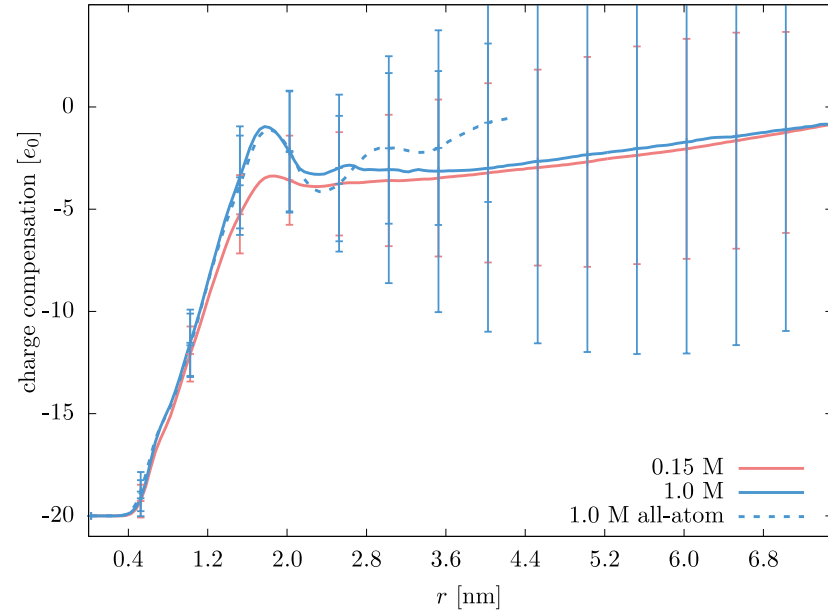
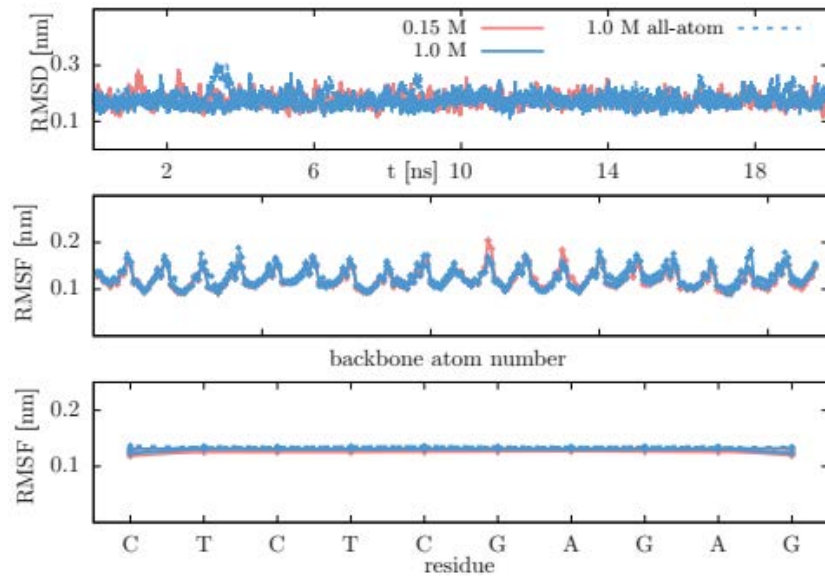
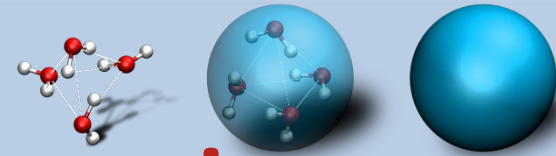


Zavadlav, Sablić, Podgornik, Praprotnik; *Biophys. J.* (2018)

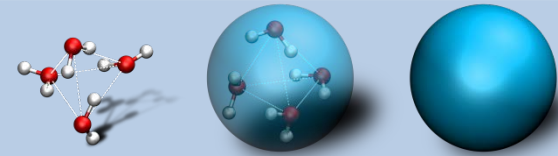
# Open Boundary Molecular Dynamics



# Open Boundary Molecular Dynamics



# Conclusions

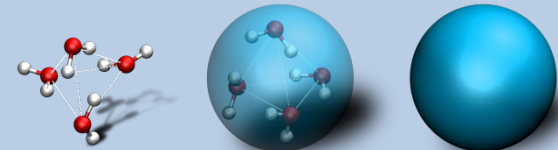


## ➤ OBMD:

- Allows for simulation of open systems that can exchange mass, energy, and linear momentum with the environment.
- Enables us to perform efficient molecular dynamics simulations of molecular liquids in the grand-canonical ensemble or under non-equilibrium flows.
- In the explicit domain, the water molecules and ions are both overtly present in the system, whereas in the implicit water domain, only the ions are explicitly present and the water is described as a continuous dielectric medium.
- Water molecules are inserted and deleted into/from the system in the intermediate buffer domain that acts as a water reservoir to the explicit domain, with both water molecules and ions free to enter or leave the explicit domain.
- Our approach is general and allows for efficient molecular simulations of biomolecules solvated in bathing salt solutions at any ionic strength condition.



# Acknowledgements



- **Staš Bevc**; Gocan d.o.o., Slovenia
  - **Julija Zavadlav**; TUM, Germany
  - **Jurij Sablić**; National Institute of Chemistry, Slovenia
  - **Rudolf Podgornik**; University of CAS, China
  - **Siewert J. Marrink**; University of Groningen, The Netherlands
  - **Rafael Delgado-Buscalioni**; UAM, Madrid, Spain
- 
- **Slovenian Research Agency** for funding