

ESPResSo++ simulation package

Short introduction

P. Papež
T. Potisk

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1 ESPResSo++

- Requirements
- Installation
- Running simulation
- Visualization

2 Examples

- Lennard-Jones (LJ) fluid
- AdResS simulation - a liquid of tetrahedral molecules
- Open molecular dynamics simulation - SPC water

Requirements

- cmake (≥ 3.12), make, g++ compiler, OpenMPI, Boost (≥ 1.69), FFTW3
- python3 modules: mpi4py ($\geq 3.0.0$), pyh5md, numpy, h5py, sphinx

Installation

```
1 git clone https://github.com/espressopp/espressopp.git
2 cd espressopp
3 mkdir build
4 cd build
5 cmake ..
6 make -j np
```

Running simulation

```
1 export PYTHONPATH=/home/kemijski/L17/espressopp/build:/home/
   kemijski/L17/mpi4py/build/lib.linux-x86_64-3.9:${PYTHONPATH}
2
3 mpirun -np 2 python3 script.py
```

Visualization

- VMD (<https://www.ks.uiuc.edu/Research/vmd>)
- OVITO (<https://www.ovito.org/linux-downloads>)

Part I

Lennard-Jones (LJ) fluid

Aims of the 1st part

We will **explain the .py script** for running simulation of the LJ fluid, focusing on:

- periodic boundary conditions (PBC),
- velocity Verlet algorithm,
- Verlet List,
- interactions (i.e., LJ potential),
- radial distribution function (RDF),
- velocity autocorrelation function (VACF).

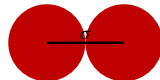
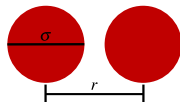
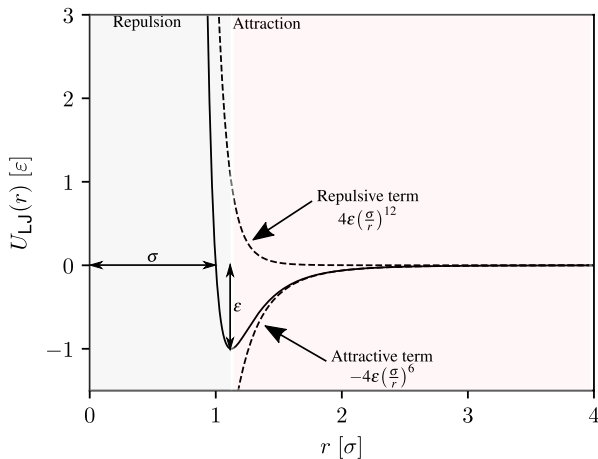
You will **perform simulation** of the LJ fluid and **analyze the results**.

We will be interested in:

- *warmup run* \rightarrow temperature (T), pressure (p), energy (E_k , E_p , E_{tot}),
- *production run* \rightarrow temperature (T), pressure (p), energy (E_k , E_p , E_{tot}), RDF, VACF.

Lennard-Jones (LJ) fluid

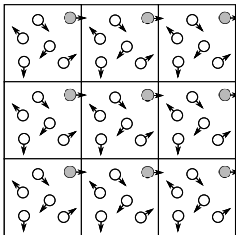
$$U_{\text{LJ}}(r) = 4\epsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right]$$



Py script

```
1 import espressopp
2 import numpy as np
3
4 # 1. specification of the main simulation parameters
5
6 Npart          = 1000
7 rho            = 0.8442
8 L              = pow(Npart/rho, 1.0/3.0)
9 box            = (L, L, L)
10 r_cutoff       = 2.5
11 skin           = 0.4
12 temperature    = 1.0
13 dt             = 0.005
14 epsilon        = 1.0
15 sigma          = 1.0
16
17 warmup_cutoff  = pow(2.0, 1.0/6.0)
18 warmup_nloops  = 100
19 warmup_isteps  = 200
20 total_warmup_steps = warmup_nloops * warmup_isteps
21 epsilon_start  = 0.1
22 epsilon_end    = 1.0
23 epsilon_delta  = (epsilon_end - epsilon_start) / warmup_nloops
24 capradius      = 0.6
25
26 equil_nloops   = 100
27 equil_isteps    = 100
```

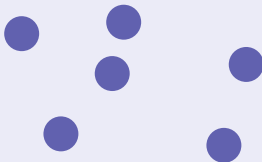
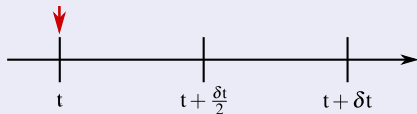
Py script



```
1 # 2. setup of the system, random number generator and
   parallelisation
2
3 system                = espressopp.System()
4 system.rng             = espressopp.esutil.RNG()
5 system.bc              = espressopp.bc.OrthorhombicBC(system.rng,box)
6 system.skin            = skin
7 NCPUs                  = espressopp.MPI.COMM_WORLD.size
8
9 nodeGrid               = espressopp.tools.decomp.nodeGrid(NCPUs,box,
   warmup_cutoff,skin)
10 cellGrid               = espressopp.tools.decomp.cellGrid(box,nodeGrid,
   warmup_cutoff,skin)
11 system.storage         = espressopp.storage.DomainDecomposition(system,
   nodeGrid,cellGrid)
```

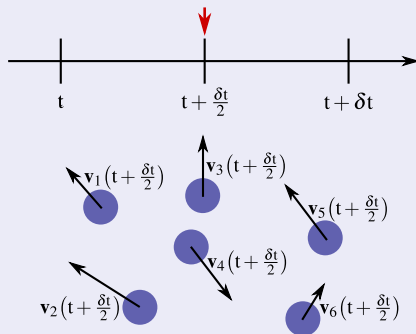
Velocity Verlet algorithm

Initial configuration



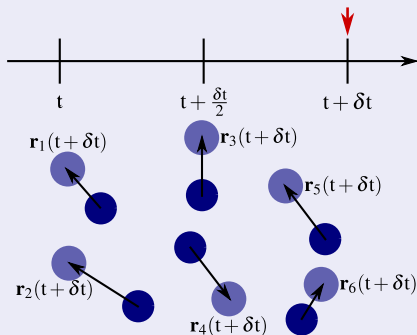
Velocity Verlet algorithm

$$\mathbf{p}_i(t + \frac{1}{2}\delta t) = \mathbf{p}_i(t) + \frac{1}{2}\delta t \mathbf{F}_i(t)$$



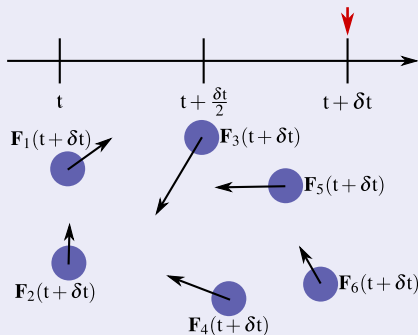
Velocity Verlet algorithm

$$\mathbf{r}_i(t + \delta t) = \mathbf{r}_i(t) + \delta t \mathbf{p}_i(t + \frac{1}{2} \delta t) / m_i$$



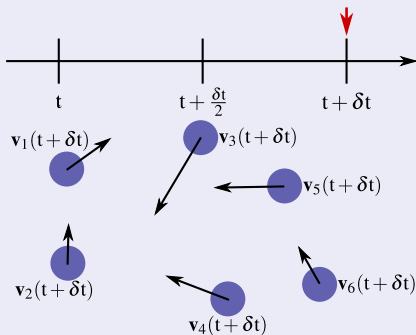
Velocity Verlet algorithm

$\mathbf{F}_i(t + \delta t)$



Velocity Verlet algorithm

$$\mathbf{p}_i(t + \delta t) = \mathbf{p}_i(t + \frac{1}{2}\delta t) + \frac{1}{2}\delta t \mathbf{F}_i(t + \delta t)$$

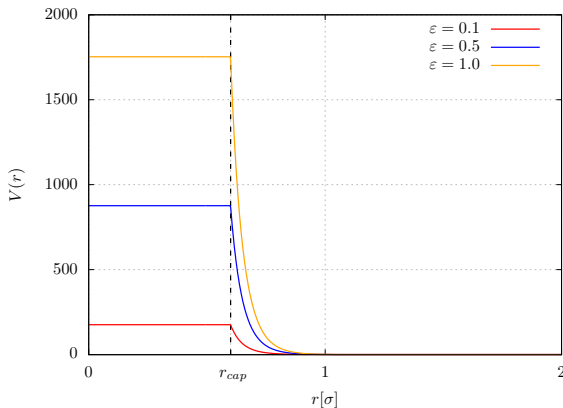


Py script

```
1 # 3. setup of the integrator and simulation ensemble
2
3 integrator      = espressopp.integrator.VelocityVerlet(system)
4 integrator.dt   = dt
5
6 if (temperature != None):
7     thermostat  = espressopp.integrator.LangevinThermostat
8     (system)
9     thermostat.gamma      = 1.0
10    thermostat.temperature = temperature
11    integrator.addExtension(thermostat)
12
13 # 4. adding particles
14 for pid in range(Npart):
15     pos = system.bc.getRandomPos()
16     system.storage.addParticle(pid, pos)
17
18 system.storage.decompose()
19
20 # 5. setting up interaction potential for the warmup
21
22 verletlist      = espressopp.VerletList(system, warmup_cutoff)
23 LJpot           = espressopp.interaction.LennardJonesCapped(epsilon=
24     epsilon_start, sigma=sigma, cutoff=warmup_cutoff,
25     caprad=capradius, shift='auto')
```

Py script

```
1 interaction = espressopp.interaction.VerletListLennardJonesCapped(  
2     verletlist)  
3 interaction.setPotential(type1=0,type2=0,potential=LJpot)
```



Py script

```
1 # 6. running the warmup loop
2
3 system.addInteraction(interaction)
4
5 fmt = '%5d %8.4f %8.4f %8.4f %8.4f %8.4f\n'
6 info_WarmUp = open('WarmUp/info_WarmUp.txt', 'w')
7
8 for step in range(1, warmup_nloops+1):
9     integrator.run(warmup_isteps)
10
11     LJpot.epsilon += epsilon_delta
12     interaction.setPotential(type1=0, type2=0, potential=LJpot)
13
14     espressopp.tools.analyse.info(system, integrator)
15     T_WarmUp = espressopp.analysis.Temperature(system).compute()
16     P_WarmUp = espressopp.analysis.Pressure(system).compute()
17     Ek_WarmUp = espressopp.analysis.KineticEnergy(system).compute()
18     Ep_WarmUp = espressopp.analysis.PotentialEnergy(system,
19         interaction).compute()
20     Etot_WarmUp = Ek_WarmUp + Ep_WarmUp
21
22     info_WarmUp.write(fmt % (step*warmup_isteps, T_WarmUp, P_WarmUp,
23         Ek_WarmUp, Ep_WarmUp, Etot_WarmUp) + '\n')
24
25 info_WarmUp.close()
26
27 system.removeInteraction(0)
28 verletlist.disconnect()
```

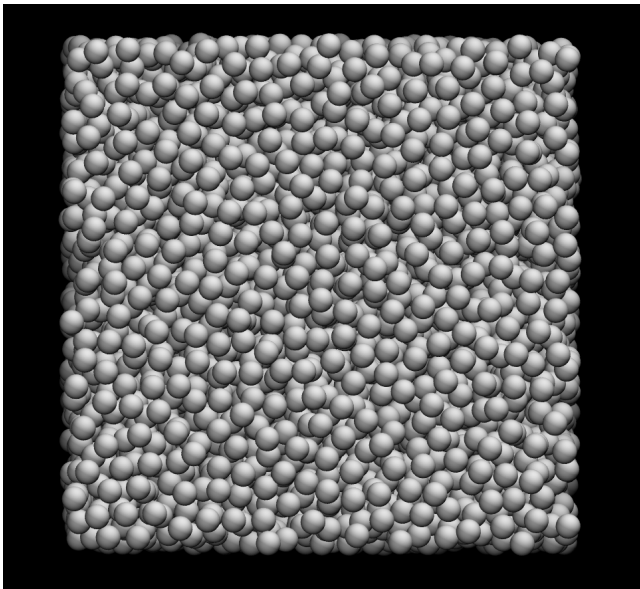
Py script

```
1 # 7. setting up interaction potential for production run
2
3 verletlist = espressopp.VerletList(system,r_cutoff)
4 interaction = espressopp.interaction.VerletListLennardJones(
5     verletlist)
6 potential = interaction.setPotential(type1=0,type2=0,potential=
7     espressopp.interaction.LennardJones(epsilon=epsilon,
8     sigma=sigma,cutoff=r_cutoff,shift=0.0))
9
10 # 8. production run
11
12 fmt = '%5d %8.4f %8.4f %8.4f %8.4f %8.4f\n'
13 info_ProductionRun = open('ProductionRun/info_ProductionRun.txt',
14     'w')
15
16 system.addInteraction(interaction)
17 system.storage.cellAdjust()
18 integrator.resetTimers()
19 integrator.step = 0
20
21 dump_conf_xyz = espressopp.io.DumpXYZ(system,integrator,
22     filename='./ProductionRun/traj.xyz')
```

Py script

```
1 for step in range(1,equil_nloops+1):
2     integrator.run(equil_isteps)
3
4     espressopp.tools.analyse.info(system, integrator)
5     T_ProductionRun = espressopp.analysis.Temperature(system).
6         compute()
7     P_ProductionRun = espressopp.analysis.Pressure(system).compute()
8     Ek_ProductionRun = espressopp.analysis.KineticEnergy(system).
9         compute()
10    Ep_ProductionRun = espressopp.analysis.PotentialEnergy(system,
11        interaction).compute()
12    Etot_ProductionRun = Ek_ProductionRun+Ep_ProductionRun
13
14    info_ProductionRun.write(fmt % (step*equil_isteps,
15        T_ProductionRun,P_ProductionRun,
16        Ek_ProductionRun,Ep_ProductionRun,
17        Etot_ProductionRun) '\n')
18    dump_conf_xyz.dump()
19
20    out_CoordVel = './ProductionRun/xyz/CoordVel_' '{num:05d}'.format
21        (num=integrator.step)+''.txt'
22    espressopp.tools.writexyz(out_CoordVel,system,velocities=True,
23        unfolded=False)
24
25    info_ProductionRun.close()
```

Snapshot of the simulated system



Perform simulation of the LJ fluid and analyze the results

- simulation:

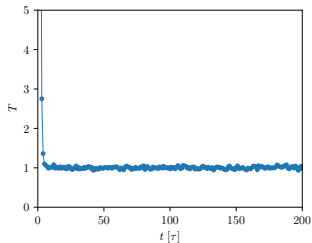
```
1 cd /home/kemijski/L17/espressopp/examples/lennard_jones
2
3 # vim lennard_jones.py # in info_ProductionRun.write() :::
  change ::: step*equil_isteps
4
5 bash run.sh # run bash script
```

- analysis:

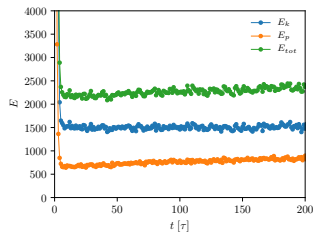
```
1 # 1. warmup run
2 cd /home/kemijski/L17/espressopp/examples/lennard_jones/WarmUp
3
4 python3 plotting.py # [T(t), P(t), Ek(t), Ep(t), Etot(t)]
5
6 # 2. production run
7 cd /home/kemijski/L17/espressopp/examples/lennard_jones/
  ProductionRun
8
9 # rsync -avP ../../WarmUp/plotting.py . # ::: some changes
10
11 python3 rdf.py # RDF
12
13 python3 green_kubo.py # VACF and D ::: vim green_kubo.py :::
  change ::: dt = 5*0.005
```

LJ fluid - results

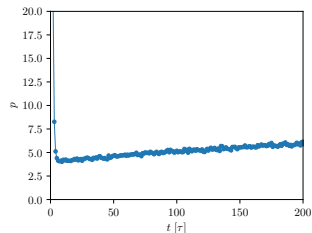
● temperature



● energy

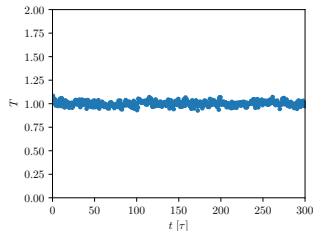


● pressure

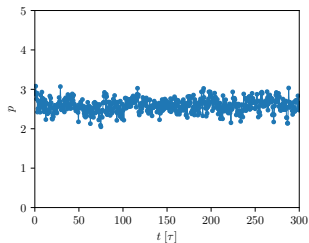


LJ fluid - results

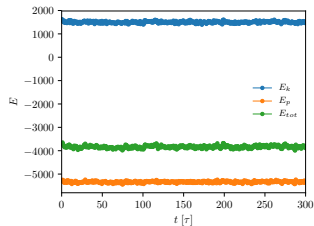
• temperature



• pressure

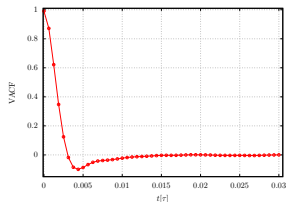


• energy



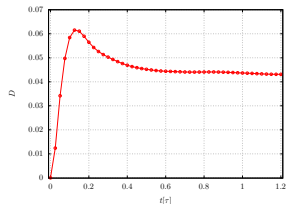
LJ fluid - results

• VACF

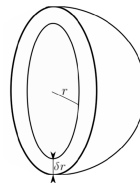


• diffusion coefficient

$$D = \frac{1}{3} \int_0^\infty dt \frac{1}{N} \sum_{i=1}^N \langle \dot{\mathbf{r}}_i(0) \cdot \dot{\mathbf{r}}_i(t) \rangle$$



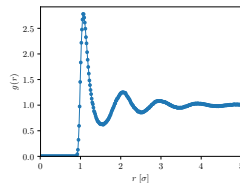
• RDF



$$V = \frac{4}{3} \pi (r + \partial r)^3 - \frac{4}{3} \pi r^3 = 4\pi r^2 \partial r + 4\pi r \partial r^2 + \frac{4}{3} \pi \partial r^3$$

$$V \approx 4\pi r^2 \partial r$$

$$\text{Number of particles: } 4\pi \rho r^2 \partial r$$



Part II

AdResS simulation
a liquid of tetrahedral molecules

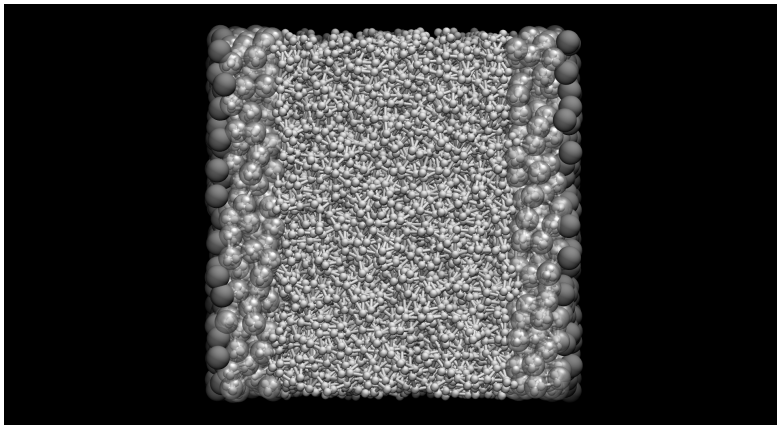
Aims of the 2nd part

We will **explain the .py script** for running multiscale simulation of a liquid of tetrahedral molecules, focusing on:

- AdResS scheme,
- system design,
- interactions (e.g., Weeks-Chandler-Andersen (WCA) potential, finite extensible nonlinear elastic (FENE) potential),
- calculation of the coarse-grained (CG) potential (using iterative Boltzmann inversion (IBI) method).

Adaptive resolution scheme

$$\mathbf{F}_{\alpha\beta} = w(\mathbf{r}_\alpha)w(\mathbf{r}_\beta)\mathbf{F}_{\alpha\beta}^{\text{AT}} + [1 - w(\mathbf{r}_\alpha)w(\mathbf{r}_\beta)]\mathbf{F}_{\alpha\beta}^{\text{CG}}$$



(1) Praprotnik, M.; Delle Site, L.; Kremer K. Adaptive resolution molecular-dynamics simulation: Changing the degrees of freedom on the fly. *J. Comput. Chem.* **2005**, *36*, 467. (2) Praprotnik, M.; Site Delle, L.; Kremer, K. Multiscale Simulation of Soft Matter: From Scale Bridging to Adaptive Resolution. *Annu. Rev. Phys. Chem.* **2008**, *59*, 545. (3) Cortes-Huerto, R.; Praprotnik, M.; Kremer, K.; Delle Site, L. From adaptive resolution to molecular dynamics of open systems. *Eur. Phys. J. B* **2021**, *94*, 189.

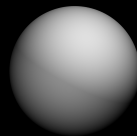
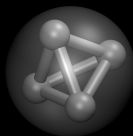
Py script

```
1 import sys
2 import time
3 import espressopp
4 import mpi4py.MPI as MPI
5 import logging
6 from espressopp import Real3D, Int3D
7 from espressopp.tools import decomp
8 from espressopp.tools import timers
9
10 # integration steps, cutoff, skin and thermostat flag
11 steps = 5000
12 timestep = 0.0001
13 intervals = 500
14
15 rc = 2.31
16 rca = 1.122462048309373
17 skin = 0.4
18
19 gamma = 0.5
20 temp = 1.0
21
22 ex_size = 12.5
23 hy_size = 5.0
```

(1) Praprotnik, M.; Delle Site, L.; Kremer K. Adaptive resolution molecular-dynamics simulation: Changing the degrees of freedom on the fly. *J. Comput. Chem.* **2005**, *36*, 467. (2) Praprotnik, M.; Delle Site, L.; Kremer K. Adaptive resolution scheme for efficient hybrid atomistic-mesoscale molecular dynamics simulations of dense liquids. *Phys. Rev. E* **2006**, *73*, 066701.

Py script

```
1 # read ESPResSo++ configuration file
2 Lx,Ly,Lz,x,y,z,type,q,vx,vy,vz,fx,fy,fz,bonds = espresso_old.read("
3                                     adress.espressopp")
4 num_particlesCG = 5001
5 num_particles = len(x)
6
7 density = num_particles/(Lx*Ly*Lz)
8 size = (Lx,Ly,Lz)
9
10 system = espressopp.System()
11 system.rng = espressopp.esutil.RNG()
12 system.bc = espressopp.bc.OrthorhombicBC(system.rng,size)
13 system.skin = skin
14
15 comm = MPI.COMM_WORLD
16 nodeGrid = decomp.nodeGrid(comm.size,size,rc,skin)
17 cellGrid = decomp.cellGrid(size,nodeGrid,rc,skin)
18
19 # AdResS domain decomposition
20 system.storage = espressopp.storage.DomainDecompositionAdress(
21     system,nodeGrid,cellGrid)
```



```
1 # prepare AT particles
2 allParticlesAT = []
3 allParticles = []
4 tuples = []
5 for pidAT in range(num_particles):
6     allParticlesAT.append([pidAT,
7                             Real3D(x[pidAT],y[pidAT],z[pidAT]),
8                             Real3D(vx[pidAT],vy[pidAT],vz[pidAT]),
9                             Real3D(fx[pidAT],fy[pidAT],fz[pidAT]),
10                                1,1.0,1])
```

Py script

```
1 # create CG particles from center of mass
2 for pidCG in range(num_particlesCG):
3     cmp = [0,0,0]
4     cmv = [0,0,0]
5     tmptuple = [pidCG+num_particles]
6     # com calculation
7     for pidAT in range(4):
8         pid = pidCG*4+pidAT
9         tmptuple.append(pid)
10        pos = (allParticlesAT[pid])[1]
11        vel = (allParticlesAT[pid])[2]
12        for i in range(3):
13            cmp[i] += pos[i]
14            cmv[i] += vel[i]
15    for i in range(3):
16        cmp[i] /= 4.0
17        cmv[i] /= 4.0
18
19    allParticles.append([pidCG+num_particles,
20                        Real3D(cmp[0],cmp[1],cmp[2]),
21                        Real3D(cmv[0],cmv[1],cmv[2]),
22                        Real3D(0, 0, 0),
23                        0,4.0,0])
24
25    pidCG_out.append(pidCG+num_particles)
```

Py script

```
1  for pidAT in range(4):
2      pid = pidCG*4+pidAT
3      allParticles.append([pid,
4                          (allParticlesAT[pid])[1],
5                          (allParticlesAT[pid])[2],
6                          (allParticlesAT[pid])[3],
7                          (allParticlesAT[pid])[4],
8                          (allParticlesAT[pid])[5],
9                          (allParticlesAT[pid])[6]])
10
11     pidAT_out.append(pid)
12
13     tuples.append(tmptuple)
14
15 # add particles
16 system.storage.addParticles(allParticles,"id","pos","v","f",
17                             "type","mass","adrat")
18
19 # add tuples
20 ftpl = espressopp.FixedTupleListAdress(system.storage)
21 ftpl.addTuples(tuples)
22 system.storage.setFixedTuplesAdress(ftpl)
23
24 # add bonds between AT particles
25 fpl = espressopp.FixedPairListAdress(system.storage,ftpl)
26 fpl.addBonds(bonds)
```

Py script

```
1 # decompose after adding tuples and bonds
2 system.storage.decompose()
3
4 # AdResS Verlet list
5 vl = espressopp.VerletListAdress(system,cutoff=rc+skin,
6     adrcut=rc+skin,dEx=ex_size,dHy=hy_size,
7     adrCenter=[18.42225,18.42225,18.42225])
8
9 # non-bonded potentials
10 # LJ Capped WCA between AT and tabulated Morse between CG particles
11 tabMorse = "pot-morse.txt"
12 potMorse = espressopp.interaction.Morse(epsilon=0.105,alpha=2.4,
13     rMin=rc,cutoff=rc,shift="auto")
14 writeTabFile(potMorse,tabMorse,N=512,low=0.005,high=4.5)
15
16 interNB = espressopp.interaction.VerletListAdressLennardJonesCapped
17     (vl,ftpl)
18 potWCA = espressopp.interaction.LennardJonesCapped(epsilon=1.0,
19     sigma=1.0,shift=True,caprad=0.27,cutoff=rca)
20 potMorse = espressopp.interaction.Tabulated(itype=2,filename=
21     tabMorse,cutoff=rc)
22 interNB.setPotentialAT(type1=1,type2=1,potential=potWCA)
23 interNB.setPotentialCG(type1=0,type2=0,potential=potMorse)
24 system.addInteraction(interNB)
```

Iterative Boltzmann inversion (IBI) method

• Inversion step

$$U_0^{eff}(r) = -k_B T \ln[g_{AT}^{cm}(r)]$$

k_B ... Boltzmann constant

T ... temperature

g_{AT}^{cm} ... RDF of the COM of CG particles (computed from the all-atom simulation)

- ▶ run CG simulation
- ▶ compute RDF (i.e., g_{CG}^i)
- ▶ correct the guess for the CG potential

• Iterative procedure

$$U_{i+1}^{eff}(r) = U_i^{eff}(r) - k_B T \ln \left[\frac{g_{CG}^i(r)}{g_{AT}^{cm}(r)} \right] \pm V_0 \left[1 - \frac{r}{r_{cut}} \right]$$

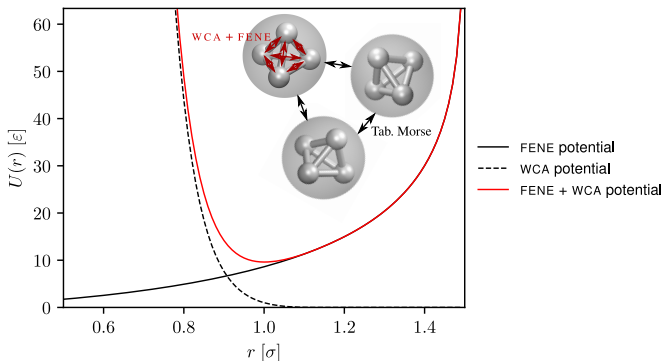
- ▶ iterate until the CG RDF matches the g_{AT}^{cm}

(1) Reith, D.; Pütz, M.; Müller-Plathe, F. Deriving effective mesoscale potentials from atomistic simulations. *J. Comput. Chem.* **2003**, *24*, 1624. (2) Bevc, S.; Junghans, C.; Praprotnik, M. STOCK: Structure mapper and online coarse-graining kit for molecular simulations. *J. Comput. Chem.* **2015**, *36*, 467.

Py script

```
1 # bonded potentials
2 # FENE and LJ potential between AT particles
3 potFENE = espressopp.interaction.FENE(K=30.0,r0=0.0,rMax=1.5)
4 potLJ = espressopp.interaction.LennardJones(epsilon=1.0,sigma=1.0,
5       shift=True,cutoff=rca)
6 interFENE = espressopp.interaction.FixedPairListFENE(system,fpl,
7       potFENE)
8 interLJ = espressopp.interaction.FixedPairListLennardJones(system,
9       fpl,potLJ)
10 system.addInteraction(interFENE)
11 system.addInteraction(interLJ)
12
13 # VV integrator
14 integrator = espressopp.integrator.VelocityVerlet(system)
15 integrator.dt = timestep
16
17 # add AdResS extension
18 adress = espressopp.integrator.Adress(system,vl,ftpl)
19 integrator.addExtension(adress)
20
21 # add Langevin thermostat extension
22 langevin = espressopp.integrator.LangevinThermostat(system)
23 langevin.gamma = gamma
24 langevin.temperature = temp
25 langevin.adress = True
26 integrator.addExtension(langevin)
```

WCA and FENE potential



Weeks-Chandler-Andersen (WCA) potential

$$U(r) = \begin{cases} 4\epsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 + \frac{1}{4} \right] & \text{if } r \leq 2^{1/6}\sigma \\ 0 & \text{if } r > 2^{1/6}\sigma \end{cases}$$

Finite extensible nonlinear elastic (FENE) potential

$$U(r) = -\frac{1}{2} r_{max}^2 K \log \left[1 - \left(\frac{r-r_0}{r_{max}} \right)^2 \right]$$

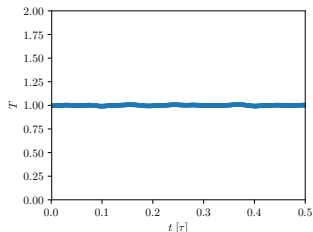
(1) Grest, G. S.; Kremer, K. Molecular dynamics simulation for polymers in the presence of a heat bath. *Phys. Rev. A* **1986**, 33, 3628.

Py script

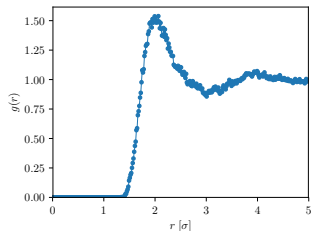
```
1 # analysis
2 temperature = espressopp.analysis.Temperature(system)
3 pressure = espressopp.analysis.Pressure(system)
4
5 fmt = '%5d %8.4f %10.5f %12.3f %12.3f %12.3f %12.3f\n'
6
7 T = temperature.compute()
8 P = pressure.compute()
9 Ek = 0.5 * T * (3 * num_particles)
10 Ep = interNB.computeEnergy()
11 Eb = interFENE.computeEnergy()
12 sys.stdout.write(' step      T      P      Pxy      etotal
13                  epotential      ebonded      ekinetic\n')
14 sys.stdout.write(fmt % (0,T,P,Ek+Ep+Eb,Ep,Eb,Ek))
15
16 nsteps = steps // intervals
17 for s in range(1, intervals + 1):
18     integrator.run(nsteps)
19     step = nsteps*s
20     T = temperature.compute()
21     P = pressure.compute()
22     Ek = 0.5 * T*(3*num_particles)
23     Ep = interNB.computeEnergy()
24     Eb = interFENE.computeEnergy()
25     sys.stdout.write(fmt % (step,T,P,Ek+Ep+Eb,Ep,Eb,Ek))
26     system.storage.decompose()
```

Liquid of tetrahedral molecules - results

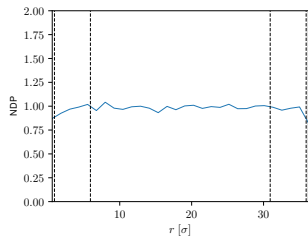
- temperature



- RDF



- normalized density profile (NDP)



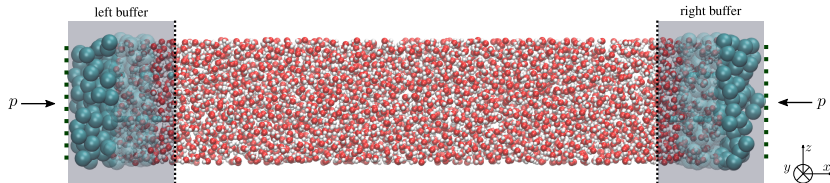
Part III

Open molecular dynamics simulation SPC water

Aims of the 3rd part

We will **explain** the **role of buffers** and **imposition of the external boundary conditions** (e.g., constant normal load) in the open boundary molecular dynamics method (OBMD).

OBMD setup



- *insertion and deletion of particles*

$$\Delta N_B = \frac{\delta t}{\tau_B} (\langle N_B \rangle - N_B)$$

$\langle N_B \rangle$... desired number of particles inside the buffer

N_B ... number of particles inside the buffer

τ_B ... relaxation time of the buffer

$\Delta N_B < 0 \rightarrow$ particles need to be deleted from the system

$\Delta N_B > 0 \rightarrow$ particles need to be inserted into the system (USHER)

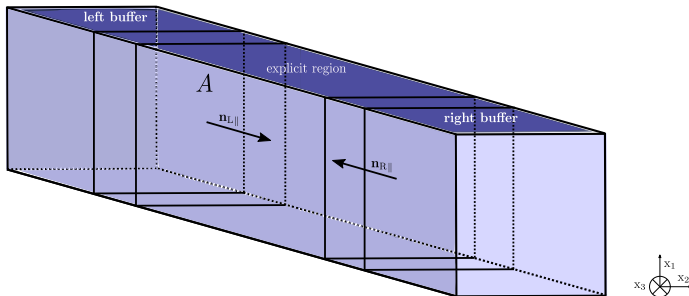
(1) Flekkøy, E. G.; Delgado-Buscalioni, R.; Coveney, P. V. Flux boundary conditions in particle simulations. *Phys. Rev. E* **2005**, *72*, 026703. (2) Delgado-Buscalioni, R.; Sablić, J.; Praprotnik, M. Open boundary molecular dynamics. *Eur. Phys. J. Spec. Top.* **2015**, *224*, 2331. (3) Delgado-Buscalioni, R.; Coveney, P. V. USHER: An algorithm for particle Insertion in dense fluids. *J. Chem. Phys.* **2003**, *119*, 978.

OBMD setup

- imposition of the external boundary condition (equilibrium)

$$\frac{\partial(\rho \mathbf{v})}{\partial t} = -\nabla \cdot \mathbf{J}^P$$

$$\mathbf{J}^P = \rho \mathbf{v} \otimes \mathbf{v} + \Pi + \tilde{\Pi}$$



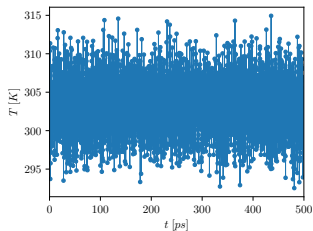
$$\Pi = (p + \pi)\mathbf{I} + \Pi^S$$

$$\Pi_{\alpha\beta}^S = -\eta(\partial_\alpha v_\beta + \partial_\beta v_\alpha - 2/3 \partial_\gamma v_\gamma \delta_{\alpha\beta})$$

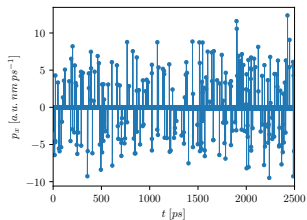
(1) De Fabritiis, G.; Serrano, M.; Delgado-Buscalioni, R.; Coveney, P. V. Fluctuating hydrodynamic modeling of fluids at the nanoscale. *Phys. Rev. E* **2007**, *75*, 026307. (2) Delgado-Buscalioni, R.; Coveney, P. V. Continuum-particle hybrid coupling for mass, momentum, and energy transfers in unsteady fluid flow. *Phys. Rev. E* **2003**, *67*, 046704. (3) Delle Site, L.; Praprotnik, M. Molecular systems with open boundaries: Theory and simulation. *Phys. Rep.* **2017**, *693*, 1.

SPC water - results

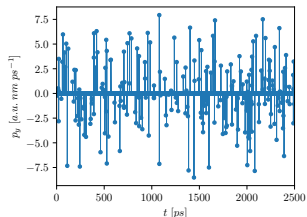
- temperature



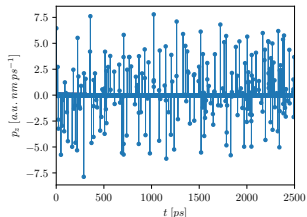
- momentum (p_x)



- momentum (p_y)

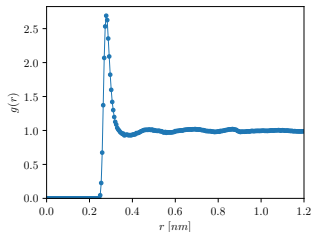


- momentum (p_z)

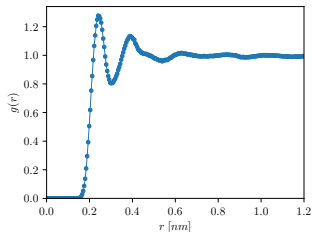


SPC water - results

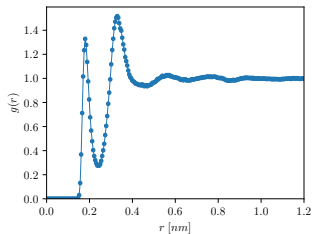
• RDF (OW-OW)



• RDF (HW-HW)



• RDF (OW-HW)



• (NDP)

